1.3b Continuity Conditions Practice Worksheet with Piecewise Functions

Use the definition of continuity to determine whether f is continuous at a. Determine type of discontinuity if function is not continuous at a

13.
$$f(x) = \begin{cases} \frac{x^2 - 4}{x - 2} & \text{if } x \neq 2\\ 5 & \text{if } x = 2 \end{cases}$$

16.
$$f(x) = \begin{cases} x - 4 & \text{if } x \le 0 \\ x^2 + x - 4 & \text{if } x > 0 \end{cases}$$

 $a = 0$

18.
$$f(x) = \begin{cases} 2 - x & \text{if } x < 1 \\ 1 & \text{if } x = 1 \\ x^2 & \text{if } x > 1 \end{cases}$$

Continuity Conditions

i. f(c) is defined

ii.
$$\lim_{x \to c} f(x)$$
 exists $(\lim_{x \to c^{-}} f(x) = \lim_{x \to c^{+}} f(x))$

$$iii. \lim_{x \to c} f(x) = f(c)$$

Find the value of "a" and/or "b" for which the function is continuous.

4)
$$f(x) = \begin{cases} 7x - 2 & \text{if } x \le 1 \\ ax^2 & \text{if } x > 1 \end{cases}$$

5)
$$f(x) = \begin{cases} ax^2 & \text{if } x \le 2\\ 2x + a & \text{if } x > 2 \end{cases}$$

6.
$$h(x) = \begin{cases} x^3; x \le 2 \\ ax^2; x > 2 \end{cases}$$

7.
$$g(x) = \begin{cases} \frac{x^2 + 3x + 2}{x + 1}; x \neq -1 \\ a; x = -1 \end{cases}$$