

Use the properties of logarithms to expand each expression to match with an equivalent one below. Then decode the answer to: Why does a moon rock taste better than an Earth rock?

1. $\log_4(xyz)$

$\log_4 x + \log_4 y + \log_4 z$

A

2. $\log_4\left(\frac{x}{yz}\right)$

$\log_4 x - \log_4 y - \log_4 z$

S

3. $\log_4 3x^4$

$\log_4 3 + \log_4 x^4$

$\log_4 3 + 4\log_4 x$

R

4. $\log_4\left(\frac{x^2y}{z}\right)$

$\log_4 x^2 + \log_4 y - \log_4 z$

$2\log_4 x + \log_4 y - \log_4 z$

M

5. $\log_4\left(\frac{3x^5}{y^2z}\right)$

$\log_4 3 + \log_4 x^5 - \log_4 y^2 - \log_4 z$

$\log_4 3 + 5\log_4 x - 2\log_4 y - \log_4 z$

O

6. $\log_4\left(\frac{6x^2y^8}{z^3}\right)$

$\log_4 6 + 2\log_4 x + 8\log_4 y - 3\log_4 z$

I

7. $\log_4\left(\frac{6y^2z^5}{x^4}\right)$

$\log_4 6 + 2\log_4 y + 5\log_4 z - 4\log_4 x$

T

8. $\log_4\left(\frac{3y^2z}{x^7}\right)$

$\log_4 3 + 2\log_4 y + \log_4 z - 7\log_4 x$

E

9. $\log_4\left(\frac{xz^6}{\sqrt{y}}\right)$

$\log_4 x + 6\log_4 z - \frac{1}{2}\log_4 y$

L

$\log_4 3 + 5\log_4 x - 2\log_4 y + \log_4 z$ P	$4\log_4 3 + 4\log_4 x$ H
8 $\log_4 3 - 7\log_4 x + 2\log_4 y + \log_4 z$ E	4 $2\log_4 x + \log_4 y - \log_4 z$ M
5 $\log_4 3 + 5\log_4 x - 2\log_4 y - \log_4 z$ O	1 $\log_4 x + \log_4 y + \log_4 z$ A
7 $\log_4 6 - 4\log_4 x + 2\log_4 y + 5\log_4 z$ T	2 $\log_4 x - \log_4 y - \log_4 z$ S
$5\log_4 3 + 5\log_4 x - 2\log_4 y - \log_4 z$ H	$\log_4 x - \log_4 y + \log_4 z$ N
6 $\log_4 6 + 2\log_4 x + 8\log_4 y - 3\log_4 z$ I	3 $\log_4 3 + 4\log_4 x$ R
$6\log_4 x - \frac{1}{2}\log_4 y + 6\log_4 z$ C	9 $\log_4 x - \frac{1}{2}\log_4 y + 6\log_4 z$ L

I T I S A L I T T L E M E T E O R
6 7 6 2 1 9 6 7 7 9 8 4 8 7 8 5 3

10.04 Solving Exponential Equations **Evens** Classwork

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$$2) \left(\frac{9}{16}\right)^{3x-2} = \left(\frac{3}{4}\right)^{5x+4}$$

$$\downarrow$$

$$\left(\frac{3}{4}\right)^{2(3x-2)} = \left(\frac{3}{4}\right)^{5x+4}$$

$$2(3x-2) = 5x+4$$

$$6x-4 = 5x+4$$

$$|x = 8$$

$$\boxed{x=8}$$

$$4) 8^x - 1 = 3.4$$

$$8^x = 4.4$$

$$\log 8^x = \log 4.4$$

$$x(\log 8) = \log 4.4$$

$$x = \frac{\log 4.4}{\log 8}$$

$$\boxed{x = 0.713}$$

$$6) \frac{2.5e^{x+4}}{2.5} = \frac{14}{2.5}$$

$$e^{x+4} = 5.6$$

$$\cancel{(x+4) \ln e} = \ln 5.6$$

$$x+4 = \ln 5.6$$

$$\boxed{x = -2.277}$$

$$\ln e^{x+4} = \ln 5.6$$

$$8) 7^{2x+1} = 3^{x+3}$$

$$\log 7^{2x+1} = \log 3^{x+3}$$

$$(2x+1)\log 7 = (x+3)\log 3$$

$$2x\log 7 + 1\log 7 = x\log 3 + 3\log 3$$

$$2x\log 7 - x\log 3 = -\log 7 + 3\log 3$$

$$x(2\log 7 - \log 3) = -\log 7 + 3\log 3$$

$$x = \frac{-\log 7 + 3\log 3}{2\log 7 - \log 3}$$

$$\boxed{x = 0.483}$$

* let $x = e^x$

$$10) e^{2x} - 15e^x + 56 = 0$$

$$* X^2 - 15x + 56 = 0$$

* factor this

$$(x - 7)(x - 8) = 0$$

↓ ↓

$$(e^x - 7)(e^x - 8) = 0$$

$$e^x - 7 = 0 \quad | \quad e^x - 8 = 0$$

$$e^x = 7 \quad | \quad e^x = 8$$

$$\ln e^x = \ln 7 \quad | \quad \ln e^x = \ln 8$$

$$x \ln e = \ln 7 \quad | \quad x \ln e = \ln 8$$

$$\boxed{x = \ln 7}$$

$$\boxed{x = \ln 8}$$

$$12) 300 = \frac{400}{1 + 3e^{-2x}}$$

~~$$\frac{300}{1} = \frac{400}{1 + 3e^{-2x}}$$~~

$$300(1 + 3e^{-2x}) = 400(1)$$

$$300 + 900e^{-2x} = 400$$

$$900e^{-2x} = 100$$

900

900

$$e^{-2x} = \frac{1}{9}$$

$$\ln e^{-2x} = \ln\left(\frac{1}{9}\right)$$

$$-2x \ln e = \ln\left(\frac{1}{9}\right)$$

$$-2x = \ln\left(\frac{1}{9}\right)$$

$$x = \frac{\ln\left(\frac{1}{9}\right)}{-2}$$

$$\boxed{x = 1.099}$$