

2.12 Quiz Review: Graphing Sec, Csc, Tan and Cot with Transformations

State the period, phase shift, and vertical shift of each function below. Then, graph at least one period of the function. Label the axes.

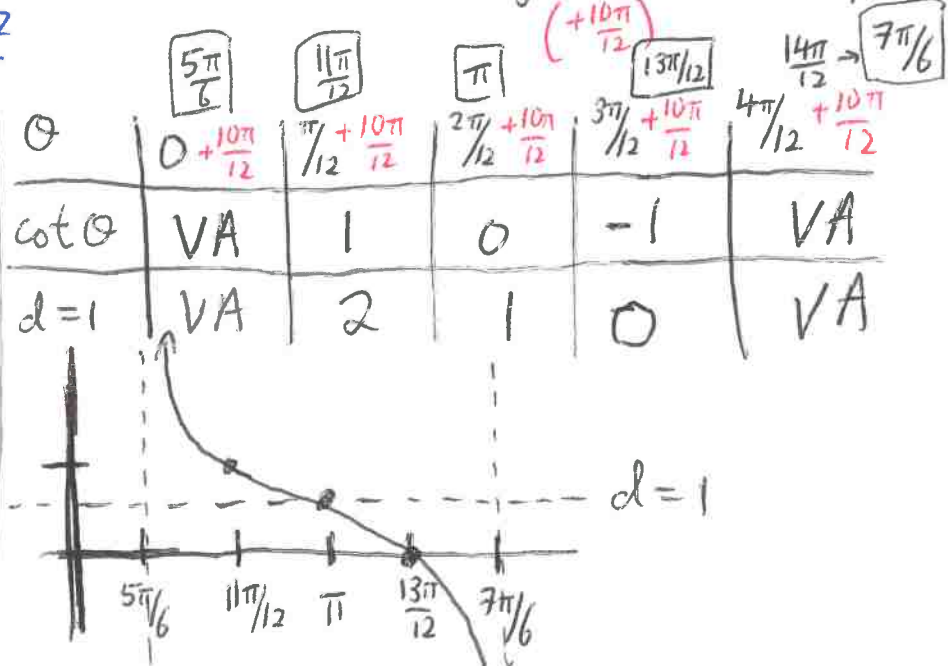
1. $y = \cot\left(3\theta - \frac{5\pi}{2}\right) + 1$

$y = \cot\left[3\left(\theta - \frac{5\pi}{3 \cdot 2}\right)\right] + 1 \rightarrow y = \cot\left[3\left(\theta - \frac{5\pi}{6}\right)\right] + 1$

Vertical Stretch: none Period: $\frac{\pi}{3}$ Interval Increments: $\frac{\pi}{12}$ Phase Shift: right $\frac{5\pi}{6}$ Vertical Shift: up 1

Asymptotes: $\frac{5\pi}{6} + \frac{\pi}{3}n, n \in \mathbb{Z}$

$b = 3$
 $P = \frac{\pi}{b} \rightarrow \frac{\pi}{3}$
 $I = \frac{P}{4} \rightarrow \frac{\pi/3}{4} \rightarrow \frac{\pi}{3} \cdot \frac{1}{4} = \frac{\pi}{12}$



think cosine

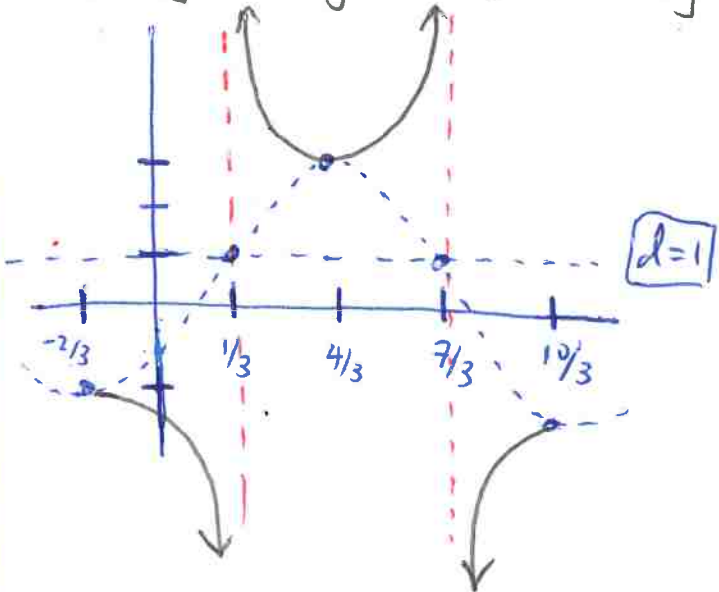
2. $y = -2\sec\left(\frac{\pi}{2}\theta + \frac{\pi}{3}\right) + 1$

Vertical Stretch: 2 Period: 4 Interval Increments: 1 Phase Shift: left $\frac{2}{3}$ Vertical Shift: up 1

Asymptotes: $\frac{1}{3} + 2n, n \in \mathbb{Z}$

$y = -2\cos\left[\frac{\pi}{2}\left(\theta + \frac{2 \cdot \pi}{\pi \cdot 3}\right)\right] + 1 \rightarrow y = -2\cos\left[\frac{\pi}{2}\left(\theta + \frac{2}{3}\right)\right] + 1$

$b = \frac{\pi}{2}$
 $P = \frac{2\pi}{b} \rightarrow \frac{2\pi}{\pi/2} \rightarrow 2\pi \cdot \frac{2}{\pi} = 4$
 $I = \frac{P}{4} \rightarrow \frac{4}{4} = 1$



θ	$0 - \frac{2}{3}$	$1 - \frac{2}{3}$	$2 - \frac{2}{3}$	$3 - \frac{2}{3}$	$4 - \frac{2}{3}$
$\cos \theta$	1	0	-1	0	1
$-2\cos \theta$	-2	0	2	0	-2
$d=1$	-1	1	3	1	-1

$$3. y = 3 \tan\left(\frac{\theta}{2} - \frac{4\pi}{3}\right) - 1 \quad y = 3 \tan\left[\frac{1}{2}\left(\theta - \frac{8\pi}{3}\right)\right] - 1 \rightarrow y = 3 \tan\left[\frac{1}{2}\left(\theta - \frac{8\pi}{3}\right)\right] - 1$$

Vertical Stretch: 3 Period: 2π Increments: $\pi/2$ Phase Shift: right $8\pi/3$ Vertical Shift: down 1

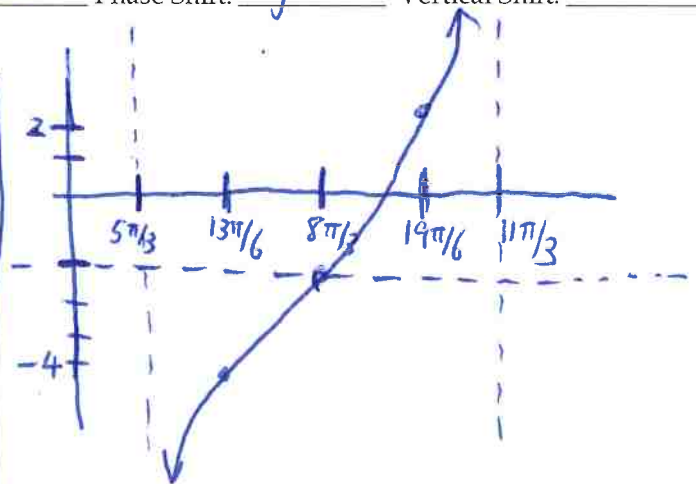
Asymptotes: $\frac{5\pi}{3} + 2\pi n, n \in \mathbb{Z}$

$$b = 1/2$$

$$P = \frac{\pi}{b} \rightarrow \frac{\pi}{1/2} = \pi \cdot \frac{2}{1} = 2\pi$$

$$I = \frac{P}{4} \rightarrow \frac{2\pi}{4} = \pi/2$$

θ	$\frac{5\pi}{3}$	$\frac{13\pi}{6}$	$\frac{8\pi}{3}$	$\frac{19\pi}{6}$	$\frac{11\pi}{3}$
	$-\pi + \frac{8\pi}{3}$	$-\pi/2 + \frac{8\pi}{3}$	$0 + \frac{8\pi}{3}$	$\pi/2 + \frac{8\pi}{3}$	$\pi + \frac{8\pi}{3}$
$\tan \theta$	VA	-1	0	1	VA
$3 \tan \theta$	VA	-3	0	3	VA
$d = -1$	VA	-4	-1	2	VA



4. Write the equation of a cotangent function with a period = $\frac{\pi}{6}$ that is shifted up 3 units and left 9π units.

$$y = a \cot[b(\theta + c)] + d$$

$$a = 1$$

$$P = \pi/6$$

$$P = \frac{\pi}{b}$$

$$\frac{\pi}{6} = \frac{\pi}{b}$$

$$b\pi = 6\pi$$

$$\underline{\underline{b = 6}}$$

$$d = 3$$

$$c = (+)9\pi$$

$$y = 1 \cot[6(\theta + 9\pi)] + 3$$