

2.2 Derivative Power Rule Practice/Review Worksheet

Derivative Power Rule:

$$\frac{d}{dx} x^n = n * x^{n-1}$$

Power Rule Conditions:

- i) All Radicals converted to Rational Exponents
- ii) All denominator variables brought up to the numerator
- iii) All parentheses resolved, all terms expanded

Finding a Derivative use the rules of differentiation to find the derivative of the function.

1) $y = x^7$

2) $y = \frac{1}{x^5}$

3) $y = \frac{3}{x^7}$

4) $f(x) = \sqrt[5]{x}$

5) $f(t) = -2t^2 + 3t - 6$

6) $y = \frac{5}{2x^2}$

7) $y = \frac{3}{2x^4}$

8) $y = \frac{6}{(5x)^3}$

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Find the derivative of the functions below:

$$9) g(t) = t^2 - \frac{4}{t^3}$$

$$10) f(x) = \frac{4x^3 + 3x^2}{x}$$

$$11) f(x) = \frac{2x^4 - x}{x^3}$$

$$12) y = x^2(2x^2 - 3x)$$

$$13) f(x) = \sqrt{x} - 6\sqrt[3]{x}$$

$$14) f(t) = t^{2/3} - t^{1/3} + 4$$

Finding an Equation of a Tangent Line In Exercises

(a) find an equation of the tangent line to the graph of f at the given point.

$$15) y = x^4 - 3x^2 + 2 \quad (1, 0)$$

$$16) y = x^3 - 3x \quad (2, 2)$$

Equation of tangent line:

- i) Find ordered pair $((x_1, y_1))$ using $f(x)$
- ii) Find slope m using $f'(x)$
- iii) $y - y_1 = m(x - x_1)$

Key

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Power Rule Conditions:

- i) All Radicals converted to Rational Exponents
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- iii) All parentheses resolved, all terms expanded

Finding a Derivative use the rules of differentiation to find the derivative of the function.

1) $y = x^7$

$$y' = 7x^6$$

2) $y = \frac{1}{x^5}$

$$y = x^{-5}$$

$$y' = -5x^{-6}$$

$$y' = \frac{-5}{x^6}$$

3) $y = \frac{3}{x^7}$

$$y = 3x^{-7}$$

$$y' = 3 \cdot 7x^{-8}$$

$$y' = \frac{-21}{x^8}$$

4) $f(x) = \sqrt[5]{x}$

$$f(x) = x^{1/5}$$

$$f'(x) = \frac{1}{5}x^{-4/5}$$

$$f'(x) = \frac{1}{5x^{4/5}}$$

5) $f(t) = -2t^2 + 3t - 6$

$$f'(t) = -4t + 3$$

6) $y = \frac{5}{2x^2}$

$$y = \frac{5}{2}x^{-2}$$

$$y' = \frac{5}{2} \cdot -2x^{-3}$$

$$y' = \frac{-5}{x^3}$$

7) $y = \frac{3}{2x^4}$

$$y = \frac{3}{2}x^{-4}$$

$$y' = \frac{3}{2} \cdot -4x^{-5}$$

$$y' = \frac{-12}{2}x^{-5}$$

$$y' = \frac{-6}{x^5}$$

8) $y = \frac{6}{(5x)^3}$

$$y = \frac{6}{5^3 x^3}$$

$$y = \frac{6}{125}x^{-3}$$

$$y' = \frac{6}{125} \cdot -3x^{-4}$$

$$y' = \frac{-18}{125}x^{-4}$$

$$y' = \frac{-18}{125x^4}$$

Derivative Power Rule:

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Power Rule Conditions:

- i) All Radicals converted to Rational Exponents
- ii) All denominator variables brought up to the numerator
- iii) All parentheses resolved, all terms expanded

Find the derivative of the functions below:

10) $g(t) = t^2 - \frac{4}{t^3}$

$g(t) = t^2 - 4t^{-3}$

$g'(t) = 2t - 4(-3t^{-4})$

$$g'(t) = 2t + \frac{12}{t^4}$$

11) $f(x) = \frac{4x^3 + 3x^2}{x}$

$f(x) = (4x^3 + 3x^2)x^{-1}$

$f(x) = 4x^2 + 3x$

$$f'(x) = 8x + 3$$

12) $f(x) = \frac{2x^4 - x}{x^3}$

$f(x) = (2x^4 - x)x^{-3}$

$f(x) = 2x^1 - x^{-2}$

$$f'(x) = 2 - (-2x^{-3})$$

$$f'(x) = 2 + \frac{2}{x^3}$$

13) $y = x^2(2x^2 - 3x)$

$y = 2x^4 - 3x^3$

$$y' = 8x^3 - 9x^2$$

14) $f(x) = \sqrt{x} - 6\sqrt[3]{x}$

$f(x) = x^{1/2} - 6x^{1/3}$

$f'(x) = \frac{1}{2}x^{-1/2} - 6 \cdot \frac{1}{3}x^{-2/3}$

$$f'(x) = \frac{1}{2x^{1/2}} - \frac{2}{x^{2/3}}$$

15) $f(t) = t^{2/3} - t^{1/3} + 4$

$f'(t) = \frac{2}{3}t^{-1/3} - \frac{1}{3}t^{-2/3}$

$$f'(t) = \frac{2}{3t^{1/3}} - \frac{1}{3t^{2/3}}$$

Finding an Equation of a Tangent Line In Exercises(a) find an equation of the tangent line to the graph of f at the given point.**Equation of tangent line:**

- i) Find ordered pair $((x_1, y_1))$ using $f(x)$
- ii) Find slope m using $f'(x)$
- iii) $y - y_1 = m(x - x_1)$

16) $y = x^4 - 3x^2 + 2$

(1, 0)

$y' = 4x^3 - 6x$

$y'(1) = 4(1)^3 - 6(1) = -2$

point: (1, 0)

slope: $m = -2$

$y - 0 = -2(x - 1)$

$$y = -2(x - 1)$$

17) $y = x^3 - 3x$

(2, 2)

$y' = 3x^2 - 3$

$y'(2) = 3(2)^2 - 3 = 9$

point: (2, 2)

slope: $m = 9$

$$y - 2 = 9(x - 2)$$