

Tell whether or not $f(x) = \sin(x)$ is an identity.

$$1. f(x) = \frac{\tan x}{\sec x} = \frac{\frac{\sin x}{\cos x}}{\frac{1}{\cos x}} \rightarrow \frac{\sin x}{\cancel{\cos x}} \cdot \frac{\cancel{\cos x}}{1} = \boxed{\sin x} \checkmark$$

Prove the following identities.

$$2. (\sin x)(\cot x + \cos x \tan x) = \cos x + \sin^2 x$$

$$\sin x \left(\frac{\cos x}{\sin x} + \cancel{\cos x} \cdot \frac{\sin x}{\cancel{\cos x}} \right) = \cos x + \sin^2 x \checkmark$$

$$3. (\cos x - \sin x)^2 = 1 - 2\sin x \cos x \checkmark$$

$$\begin{aligned} &(\cos x - \sin x)(\cos x - \sin x) \\ &\underline{\cos^2 x} - \underline{\cos x \sin x} - \underline{\sin x \cos x} + \underline{\sin^2 x} \\ &\quad - 2\sin x \cos x \end{aligned}$$

$$\boxed{1 - 2\sin x \cos x} \checkmark$$

$$4. \tan x + \sec x = \frac{\cos x}{1 - \sin x}$$

$$\frac{\sin x}{\cos x} + \frac{1}{\cos x} = \frac{\sin x + 1}{\cos x \cdot \underline{\cos x}}$$

$$\left| \frac{(\sin x + 1)(\cos x)}{\cos^2 x} \rightarrow \frac{(\cancel{\sin x + 1})(\cos x)}{\frac{1 - \sin^2 x}{(1 - \sin x)(1 + \sin x)}} \right.$$

$$\left. \frac{\cos x}{1 - \sin x} \checkmark \right.$$

$$5. \frac{\sec^2 \theta - 1}{\sin \theta} = \frac{\sin \theta}{1 - \sin^2 \theta}$$

$$\frac{\tan^2 \theta}{\sin \theta} \rightarrow \frac{\frac{\sin^2 \theta}{\cos^2 \theta}}{\sin \theta}$$

$$\frac{\sin \theta}{\cos^2 \theta} \cdot \frac{1}{\cancel{\sin \theta}} \rightarrow \frac{\sin \theta}{\cos^2 \theta}$$

$$\frac{\sin \theta}{1 - \sin^2 \theta} \leftarrow$$

$$6. \frac{1}{1-\cos x} + \frac{1}{1+\cos x} = 2\csc^2 x$$

$$\frac{1+\cos x}{(1-\cos x)(1+\cos x)} + \frac{1-\cos x}{(1-\cos x)(1+\cos x)}$$

$$\frac{2}{(1-\cos x)(1+\cos x)} \rightarrow \frac{2}{1-\cos^2 x} \rightarrow \frac{2}{\sin^2 x}$$

$$\frac{2}{\frac{1}{\csc^2 x}} = 2 \cdot \frac{\csc^2 x}{1} = \boxed{2\csc^2 x}$$

$$7. \sin^2 \alpha - \cos^2 \alpha = 1 - 2\cos^2 \alpha$$

$$(1 - \cos^2 \alpha) - \cos^2 \alpha = 1 - 2\cos^2 \alpha \checkmark$$

pythagorean Identity

$$8. \frac{1}{\tan \beta} + \frac{\tan \beta}{1} = \sec \beta \csc \beta \checkmark$$

$$\frac{1}{\tan \beta} + \frac{\tan^2 \beta}{\tan \beta} \quad \left| \quad \frac{\sec^2 \beta}{\tan \beta} \right.$$

$$\frac{1 + \tan^2 \beta}{\tan \beta} \quad \left| \quad \frac{\sec^2 \beta}{\frac{\sin \beta}{\cos \beta}} \right.$$

$$\sec^2 \beta \cdot \frac{\cos \beta}{\sin \beta}$$

$$\sec^2 \beta \cdot \left[\frac{1}{\sec \beta} \cdot \frac{1}{\csc \beta} \right] \rightarrow \frac{1}{\sec \beta} \cdot \frac{\csc \beta}{1}$$

$$\sec \beta \cdot \frac{\csc \beta}{\cancel{\sec \beta}} \rightarrow \sec \beta \csc \beta \checkmark$$

Accelerated Pre-Calculus

Name: _____

4.04 Verifying Identities Classwork Day 2

Date: _____ Period: _____

Prove the following identities.

$$1. \frac{\sec x + 1}{\tan x} = \frac{\sin x}{1 - \cos x}$$

In Exercises 17–22, simplify the expression to either 1 or -1.

17. $\sin x \csc(-x) \rightarrow (\sin x)(-\csc x) = \cancel{\sin x} \cdot \frac{-1}{\cancel{\sin x}} = -1$

18. $\sec(-x) \cos(-x)$

19. $\cot(-x) \cot(\pi/2 - x) (-\cot x)(\tan x) = \boxed{-1}$

20. $\cot(-x) \tan(-x)$

21. $\sin^2(-x) + \cos^2(-x) \left[\sin(-x) \right]^2 + \left[\cos(-x) \right]^2 \left| \sin^2 x + \cos^2 x \right. = \boxed{1}$

22. $\sec^2(-x) - \tan^2 x$

$\left[-\sin x \right]^2 + \left[\cos x \right]^2$

In Exercises 23–26, simplify the expression to either a constant or a basic trigonometric function. Support your result graphically.

23. $\frac{\tan(\pi/2 - x) \csc x}{\csc^2 x} \rightarrow \frac{(\cot x)(\cancel{\csc x})}{\csc^2 x}$

$\frac{\frac{\cos x}{\sin x}}{\frac{1}{\sin x}} \rightarrow \frac{\cos x}{\cancel{\sin x}} \cdot \frac{\cancel{\sin x}}{1} = \boxed{\cos x}$