

1) Find the Sum  $\sum_{k=3}^6 \frac{5}{2^k - 3k^2}$

2) Use Sigma Notation to write the sum  $\frac{2}{2-3} + \frac{3}{2-9} + \frac{4}{2-27} + \dots + \frac{8}{2-2187}$

3) Use properties of summation to evaluate the sum:

$$\sum_{i=1}^{31} 2(i-1)^2$$

4) Use Left, Middle, and Right endpoints to find approximations of area of region between the graph and the x-axis:  $f(x) = 1 + 3x^2$  in interval  $[1, 5]$  using 3 rectangles

a) Left endpoint (LRAM):

b) Right Endpoint(RRAM):

c) Middle rectangle (MRAM):

5) Selected values of a function,  $f$ , are given in the table below:

x	1	2	5	7	8	12	15	19	22
$f(x)$	2	3	7	4	11	19	8	1	5

- a) Give the middle approximation with 2 subintervals for  $f$  on the interval  $[1, 22]$

x	1	2	5	7	8	12	15	19	22
$f(x)$	2	3	7	4	11	19	8	1	5

- b) Use right-handed rectangles to approximate the area with 3 subintervals for  $f$  on the interval  $[2, 19]$

x	1	2	5	7	8	12	15	19	22
$f(x)$	2	3	7	4	11	19	8	1	5

- c) Use left-handed rectangles to approximate the area with 4 subintervals for  $f$  on the interval  $[7, 19]$

x	1	2	5	7	8	12	15	19	22
$f(x)$	2	3	7	4	11	19	8	1	5

- d) Use trapezoids to approximate the area with 3 subintervals for  $f$  on the interval  $[5, 22]$

1) Find the Sum  $\sum_{k=3}^6 \frac{5}{2^k - 3k^2}$

$$\frac{5}{2^3 - 3(3)^2} + \frac{5}{2^4 - 3(4)^2} + \frac{5}{2^5 - 3(5)^2} + \frac{5}{2^6 - 3(6)^2} = \frac{-5}{19} + \frac{-5}{32} + \frac{-5}{43} + \frac{-5}{44} = \boxed{-0.649}$$

2) Use Sigma Notation to write the sum  $\frac{2}{2-3} + \frac{3}{2-9} + \frac{4}{2-27} + \dots + \frac{8}{2-2187}$

$$\sum_{i=1}^7 \frac{i+1}{2-3^i}$$

3) Use properties of summation to evaluate the sum:

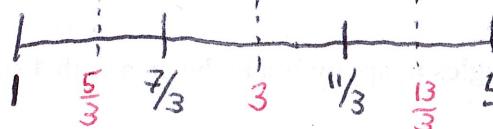
$$\sum_{i=1}^{31} 2(i-1)^2 = \sum 2(i-1)(-1) = \sum 2(i^2 - 2i + 1) = \sum 2i^2 - 4i + 2$$

$$\sum 2i^2 - \sum 4i + \sum 2$$

$2 \left[ \sum i^2 \right] - 4 \left[ \sum i \right] + 2 \left[ \sum 1 \right]$	$\left  \begin{array}{l} 2 \left[ \frac{n(n+1)(2n+1)}{6} \right] - 4 \left[ \frac{n(n+1)}{2} \right] + 2[n] \\ 2 \left[ \frac{(31)(32)(63)}{6} \right] - 4 \left[ \frac{31(32)}{2} \right] + 2(31) \end{array} \right $	$\begin{array}{r} 20832 \\ -1982 \\ +62 \\ \hline 18910 \end{array}$
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4) Use Left, Middle, and Right endpoints to find approximations of area of region between the graph and the x-axis:  $f(x) = 1 + 3x^2$  in interval  $[1, 5]$  using 3 rectangles

$$w = \frac{b-a}{n} = \frac{5-1}{3} = \frac{4}{3}$$



$$1 + \frac{7}{3} = \frac{10}{3} \cdot \frac{1}{2} = \frac{5}{3}$$

$$\frac{7}{3} + \frac{11}{3} = \frac{18}{3} \cdot \frac{1}{2} = 3$$

$$\frac{11}{3} + 5 = \frac{26}{3} \cdot \frac{1}{2} = \frac{13}{3}$$

a) Left endpoint (LRAM):

$$\text{Area} \approx \frac{4}{3} \cdot f(1) + \frac{4}{3} \cdot f\left(\frac{5}{3}\right) + \frac{4}{3} \cdot f\left(\frac{11}{3}\right)$$

$$= \frac{4}{3} \left[ 4 + \frac{5^2}{3} + \frac{124}{3} \right]$$

$$= \frac{752}{9} \approx 83.556$$

b) Right Endpoint(RRAM):

$$\text{Area} \approx \frac{4}{3} \left[ f\left(\frac{5}{3}\right) + f\left(\frac{11}{3}\right) + f(5) \right]$$

$$= \frac{4}{3} \left[ \frac{5^2}{3} + \frac{124}{3} + 76 \right]$$

$$= \frac{1616}{9} \approx 179.556$$

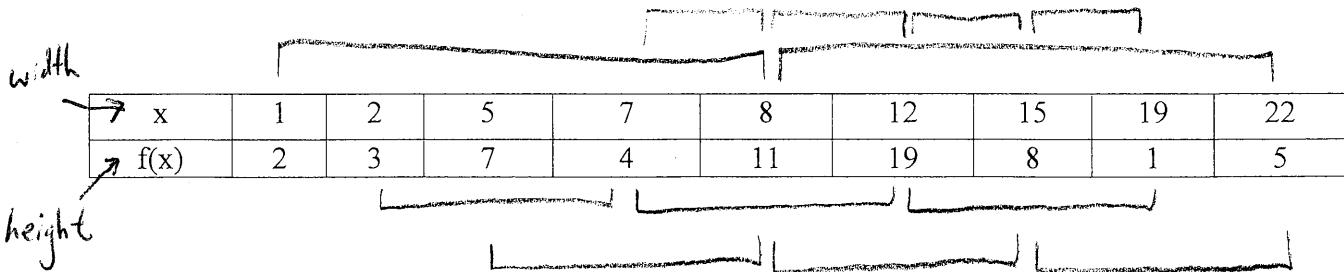
c) Middle rectangle (MRAM):

$$\text{Area} \approx \frac{4}{3} \left[ f\left(\frac{5}{3}\right) + f(3) + f\left(\frac{13}{3}\right) \right]$$

$$= \frac{4}{3} \left[ \frac{28}{3} + 28 + \frac{172}{3} \right]$$

$$= \frac{1136}{9} \approx 126.222$$

- 5) Selected values of a function,  $f$ , are given in the table below:



- a) Give the middle approximation with 2 subintervals for  $f$  on the interval  $[1, 22]$

$$\begin{aligned} \text{Area} &\approx 7 \cdot f(5) + 14 \cdot f(15) \\ &= 7(7) + 14(8) \end{aligned} \quad \left| \begin{array}{l} = 49 + 112 \\ = 161 \end{array} \right.$$

- b) Use right-handed rectangles to approximate the area with 3 subintervals for  $f$  on the interval  $[2, 19]$

$$\begin{aligned} A &\approx 5 \cdot f(7) + 5 \cdot f(12) + 7 \cdot f(19) \\ &= 5(4) + 5(19) + 7(1) \end{aligned} \quad \left| \begin{array}{l} = 20 + 95 + 7 \\ = 122 \end{array} \right.$$

- c) Use left-handed rectangles to approximate the area with 4 subintervals for  $f$  on the interval  $[7, 19]$

$$\begin{aligned} A &\approx 1 \cdot f(7) + 4 \cdot f(8) + 3 \cdot f(12) + 4 \cdot f(15) \\ &= 1(4) + 4(11) + 3(19) + 4(8) = 137 \end{aligned}$$

- d) Use trapezoids to approximate the area with 3 subintervals for  $f$  on the interval  $[5, 22]$

$$* \text{Trapezoid Area} = \frac{W}{2} [h_1 + h_2]$$

$$\begin{aligned} A &\approx \frac{3}{2} [f(5) + f(8)] + \frac{7}{2} [f(8) + f(15)] + \frac{7}{2} [f(15) + f(22)] \\ &= \frac{3}{2} [7 + 11] + \frac{7}{2} [11 + 8] + \frac{7}{2} [8 + 5] \\ &= 27 + 66.5 + 45.5 = 139 \end{aligned}$$