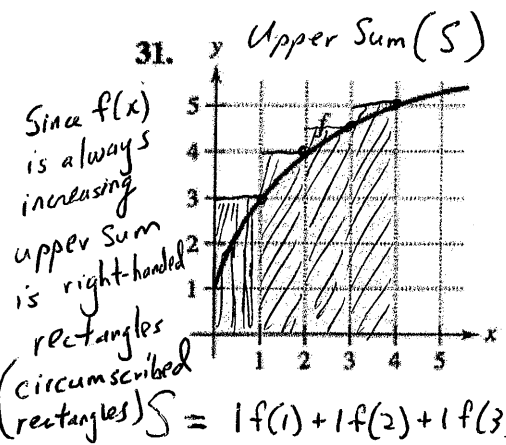


Ch. 4.2 Homework Problems

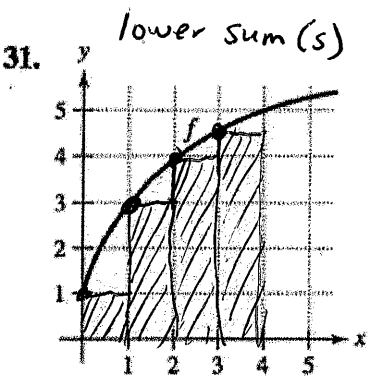
Using Upper and Lower Sums In Exercises 31 and 32, bound the area of the shaded region by approximating the upper and lower sums. Use rectangles of width 1.



$$S = 1f(1) + 1f(2) + 1f(3) + 1f(4)$$

$$= 1(3) + 1(4) + 1(4.5) + 1(5)$$

$$S = \frac{33}{2} \text{ or } 16.5$$



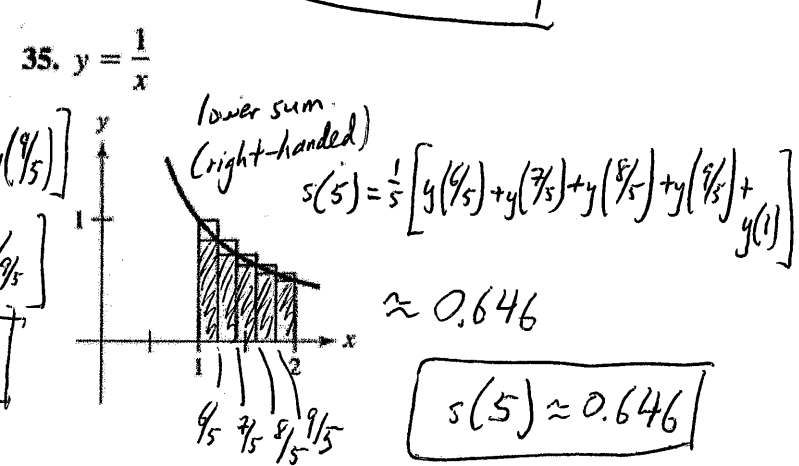
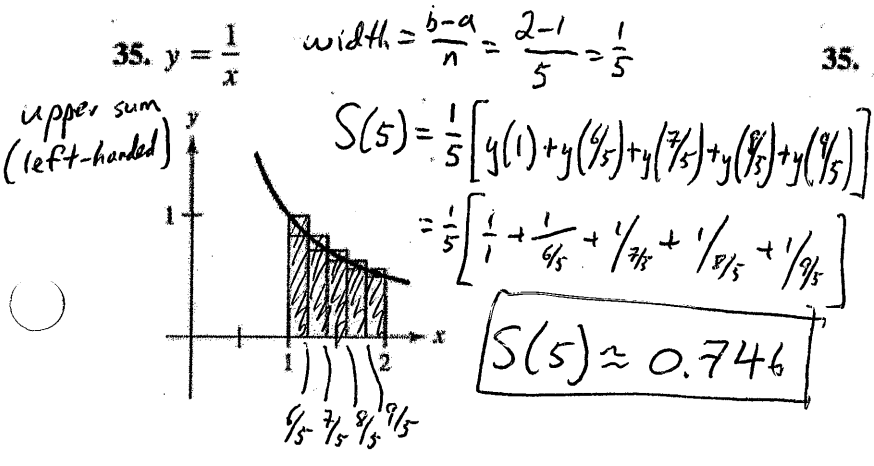
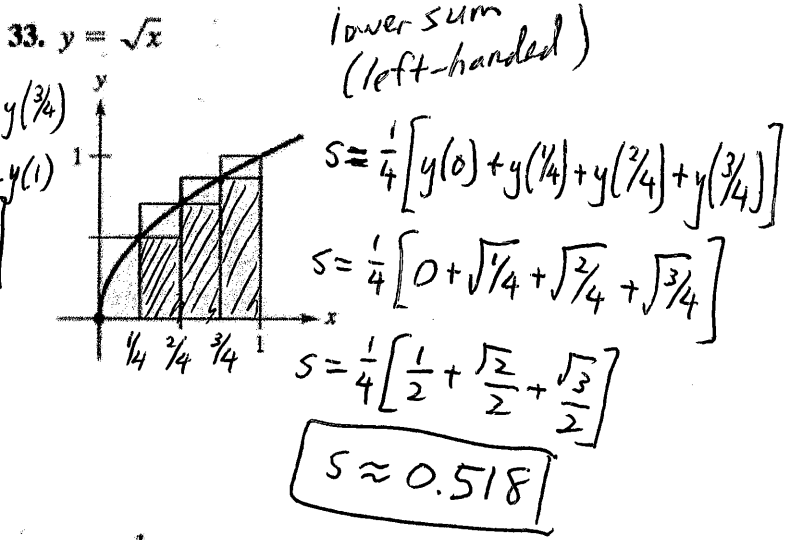
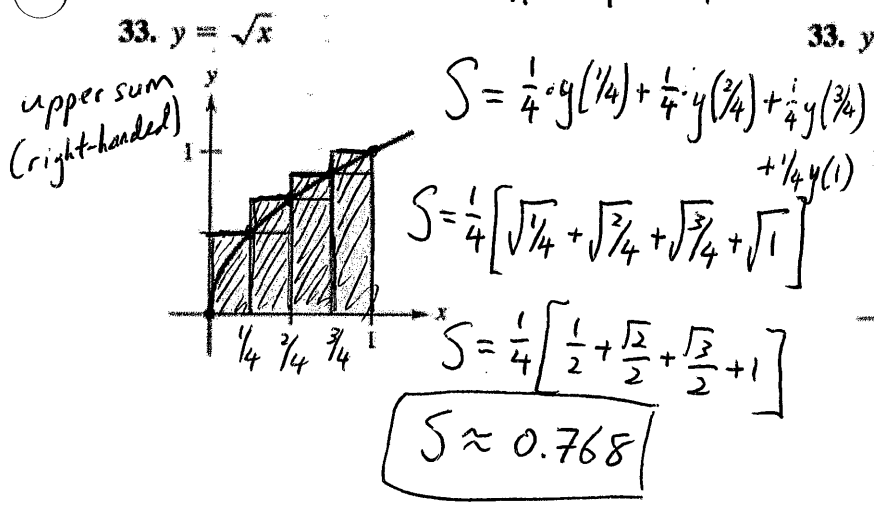
$$s = 1f(0) + 1f(1) + 1f(2) + 1f(3)$$

$$s = 1(1) + 1(3) + 1(4) + 1(4.5)$$

$$s = \frac{25}{2} = 12.5$$

Finding Upper and Lower Sums for a Region In Exercises 33-36, use upper and lower sums to approximate the area of the region using the given number of subintervals (of equal width).

$$\text{width} = \frac{b-a}{n} = \frac{1-0}{4} = \frac{1}{4}$$



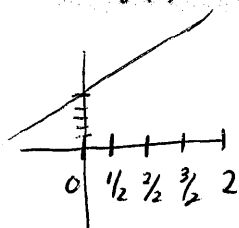
Ch. 4.2 Continued

Approximating the Area of a Plane Region In Exercises 25–30, use left and right endpoints and the given number of rectangles to find two approximations of the area of the region between the graph of the function and the x-axis over the given interval.

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25. $f(x) = 2x + 5$, $[0, 2]$, 4 rectangles

$$\text{width} = \frac{b-a}{n} = \frac{2-0}{4} = \frac{1}{2}$$

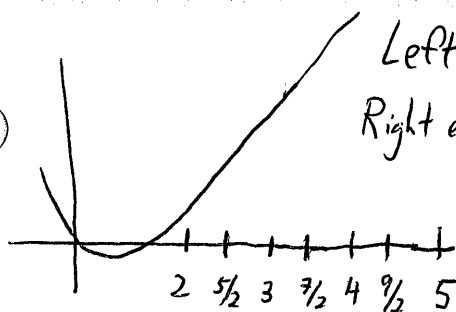


$$\text{Left endpoint: } A = \frac{1}{2} [f(0) + f(1/2) + f(1) + f(3/2)] = \frac{1}{2} [5 + 6 + 7 + 8] = \frac{26}{2} = \boxed{13}$$

$$\text{Right endpoint: } A = \frac{1}{2} [f(1/2) + f(1) + f(3/2) + f(2)] = \frac{1}{2} (6 + 7 + 8 + 9) = \frac{30}{2} = \boxed{15}$$

27. $g(x) = 2x^2 - x - 1$, $[2, 5]$, 6 rectangles

$$\text{width} = \frac{b-a}{n} = \frac{5-2}{6} = \frac{3}{6} = \frac{1}{2}$$

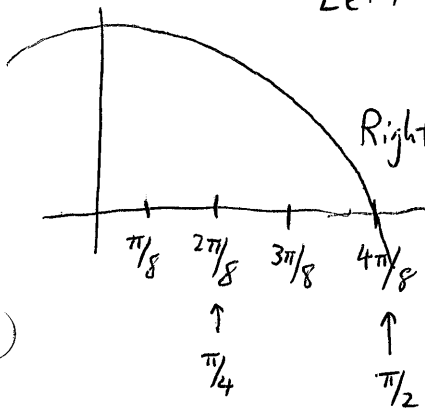


$$\text{Left endpoint: } A = \frac{1}{2} [f(2) + f(5/2) + f(3) + f(7/2) + f(4) + f(9/2)] = \boxed{55}$$

$$\text{Right endpoint: } A = \frac{1}{2} [f(5/2) + f(3) + f(7/2) + f(4) + f(9/2) + f(5)] = \boxed{74.5}$$

29. $f(x) = \cos x$, $[0, \frac{\pi}{2}]$, 4 rectangles

$$\text{width} = \frac{b-a}{n} = \frac{\pi/2 - 0}{4} = \frac{\pi}{8}$$

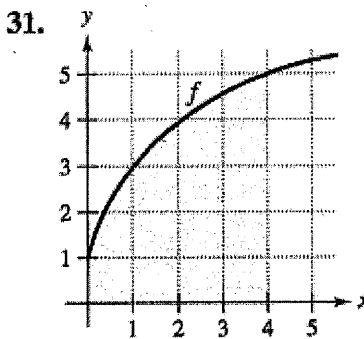
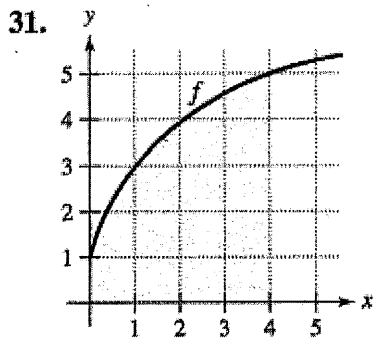


$$\text{Left endpoint: } \frac{\pi}{8} [f(0) + f(\pi/8) + f(\pi/4) + f(3\pi/8)] \approx \boxed{1.1835}$$

$$\text{Right endpoint: } \frac{\pi}{8} [f(\pi/8) + f(\pi/4) + f(3\pi/8) + f(\pi/2)] \approx \boxed{0.7908}$$

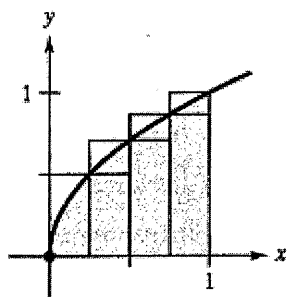
Ch. 4.2 Homework Problems

Using Upper and Lower Sums In Exercises 31 and 32, bound the area of the shaded region by approximating the upper and lower sums. Use rectangles of width 1.

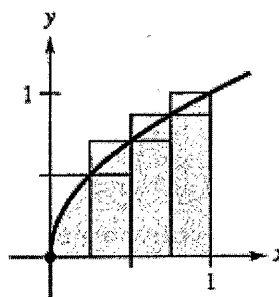


Finding Upper and Lower Sums for a Region In Exercises 33–36, use upper and lower sums to approximate the area of the region using the given number of subintervals (of equal width).

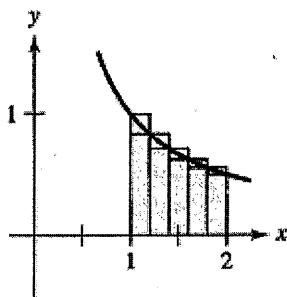
33. $y = \sqrt{x}$



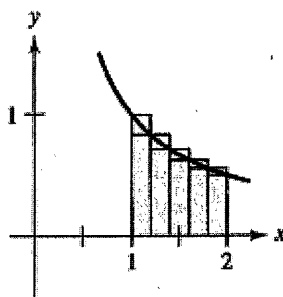
33. $y = \sqrt{x}$



35. $y = \frac{1}{x}$



35. $y = \frac{1}{x}$



Approximating the Area of a Plane Region In Exercises 25–30, use left and right endpoints and the given number of rectangles to find two approximations of the area of the region between the graph of the function and the x -axis over the given interval.

25. $f(x) = 2x + 5$, $[0, 2]$, 4 rectangles

27. $g(x) = 2x^2 - x - 1$, $[2, 5]$, 6 rectangles

29. $f(x) = \cos x$, $\left[0, \frac{\pi}{2}\right]$, 4 rectangles