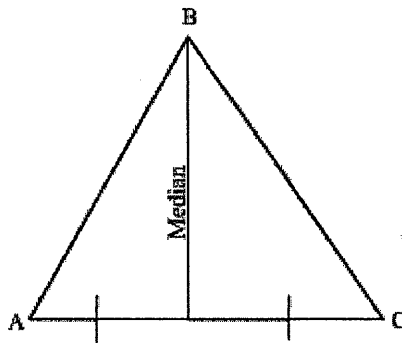


Geometry
Points of Concurrency Notes
Centroid and Orthocenter

Key

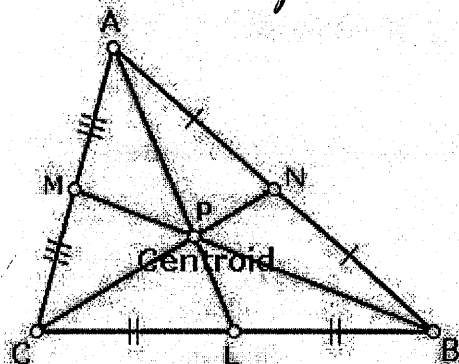
Essential Question 1: What are the properties of a median?

- A median of a triangle is a segment whose endpoints are a vertex of the triangle and the midpoint of the opposite side.



- The point of concurrency of the **medians of a triangle** is called the centroid of the triangle.
- The centroid is the concurrency point of the triangle

Theorem: The medians of a triangle intersect at a point that is two-thirds of the distance from each vertex to the midpoint of the opposite side

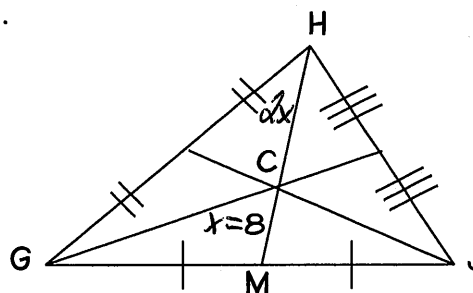


The centroid is point of concurrency inside the triangle.

Example 1: C is the centroid of $\triangle GHJ$ and $CM = 8$. Find CH and HM.

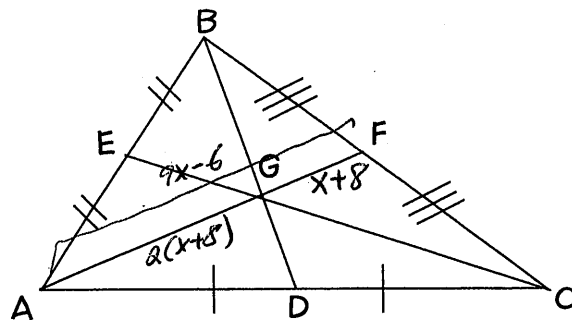
$$CH = 2(8) = 16$$

$$HM = 16 + 8 = 24$$



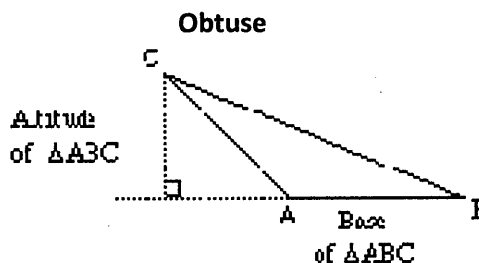
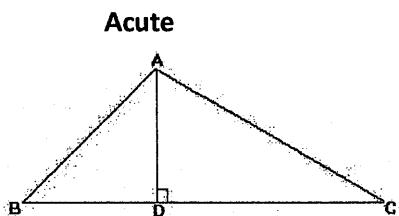
Example 2: G is the centroid of $\triangle ABC$. Find the value of x given $FG = x + 8$ and $AG = 9x - 6$.

$$\begin{aligned}
 2(x+8) + x+8 &= 9x-6 \\
 2x+16+x+8 &= 9x-6 \\
 3x+24 &= 9x-6 \\
 30 &= 6x \\
 \boxed{5} &= x
 \end{aligned}$$



Essential Question 2: What are the properties of an altitude?

- An altitude of a triangle is the perpendicular segment from a vertex to the opposite side or to the line that contains the opposite side.



- Another word for the altitude of a triangle is the height of the triangle.
- The point of concurrency of the **altitudes of a triangle** is called the orthocenter of the triangle.

