

Key

7.03 Quiz Review:

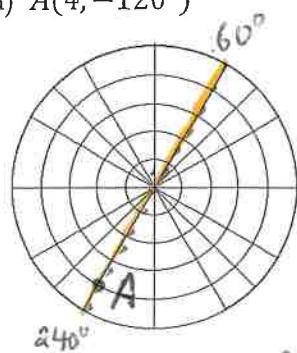
Date _____

Polar Coordinates, Equations, and Distance

- 1) Graph each point on the polar grid. Find three other pairs of polar coordinates that name the point

$$\text{if } -360^\circ \leq \theta \leq 360^\circ \rightarrow \theta = -120^\circ + 360^\circ = 240^\circ$$

a) $A(4, -120^\circ)$

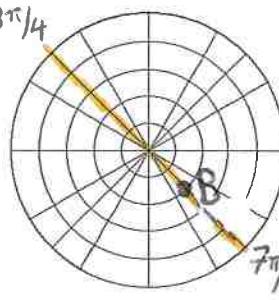


$$\begin{aligned} &(4, 240^\circ) \\ &(-4, 60^\circ) \\ &(-4, -300^\circ) \end{aligned}$$

$$\text{if } -2\pi \leq \theta \leq 2\pi$$

$$\frac{7\pi}{4} - 2\pi \rightarrow \frac{7\pi}{4} - \frac{8\pi}{4} = -\frac{\pi}{4}$$

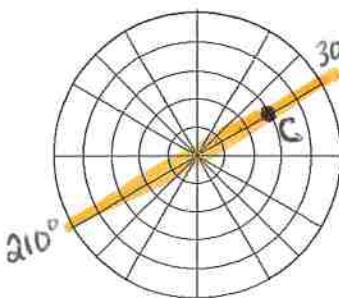
b) $B(2, \frac{7\pi}{4})$



$$(2, -\frac{\pi}{4})$$

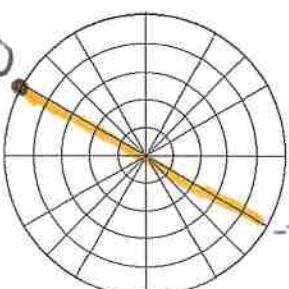
$$\begin{aligned} &(-2, \frac{3\pi}{4}) \\ &(-2, -\frac{5\pi}{4}) \end{aligned}$$

c) $C(-3, 210^\circ)$



$$\begin{aligned} &(-3, -150^\circ) \\ &(3, 30^\circ) \\ &(3, -330^\circ) \end{aligned}$$

d) $D(-5, -\frac{\pi}{6})$



$$(-5, \frac{11\pi}{6})$$

$$\begin{aligned} &(5, \frac{5\pi}{6}) \\ &(5, -\frac{7\pi}{6}) \end{aligned}$$

- 2) Given the polar distance formula between two points $A(r_1, \theta_1)$ and $B(r_2, \theta_2)$:

$$AB = \sqrt{r_1^2 + r_2^2 - 2r_1r_2 \cos(\theta_2 - \theta_1)}, \text{ find the distance between } A \text{ and } B.$$

a) $A(4, 200^\circ) \quad B(-3, 60^\circ)$

*degrees
mode

$$\begin{aligned} &= \sqrt{4^2 + 3^2 - 2(4)(-3) \cos(60^\circ - 200^\circ)} \\ &= \sqrt{25 + 24 \cos(-140^\circ)} \end{aligned}$$

a) $AB = \underline{2.572 \text{ units}}$

b) $A(-7, \frac{5\pi}{6}) \quad B(2, -\frac{4\pi}{3})$ * Radian Mode

$$\begin{aligned} &= \sqrt{7^2 + 2^2 - 2(-7)(2) \cos\left(-\frac{4\pi}{3} - \frac{5\pi}{6}\right)} \\ &= \sqrt{53 + 28 \cos\left(-\frac{13\pi}{6}\right)} \end{aligned}$$

b) $AB = \underline{8.789 \text{ units}}$

$$(r \cos \theta, r \sin \theta)$$

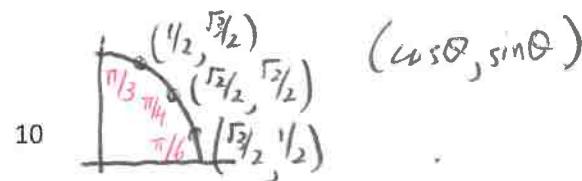
3) Find the rectangular coordinates for each point with the given polar coordinates. Answer in exact form.

a) $\left(5, \frac{5\pi}{3}\right) \quad \left(5 \cos \frac{5\pi}{3}, 5 \sin \frac{5\pi}{3}\right)$
 $\left(5\left(\frac{1}{2}\right), 5\left(-\frac{\sqrt{3}}{2}\right)\right)$

a) $\left(\frac{5}{2}, -\frac{5\sqrt{3}}{2}\right)$

c) $\left(8, \frac{7\pi}{6}\right) \quad \left(8 \cos \frac{7\pi}{6}, 8 \sin \frac{7\pi}{6}\right)$
 $\left(8\left(-\frac{\sqrt{3}}{2}\right), 8\left(-\frac{1}{2}\right)\right)$

c) $(-4\sqrt{3}, -4)$



b) $\left(-6, \frac{3\pi}{4}\right) \quad \left(-6 \cos \frac{3\pi}{4}, -6 \sin \frac{3\pi}{4}\right)$
 $\left(-6\left(-\frac{\sqrt{2}}{2}\right), -6\left(\frac{\sqrt{2}}{2}\right)\right)$

b) $(3\sqrt{2}, -3\sqrt{2})$

d) $\left(-12, -\frac{3\pi}{2}\right) \rightarrow \theta = -\frac{3\pi}{2} + 2\pi = \frac{\pi}{2}$

$\left(-12 \cos \frac{\pi}{2}, -12 \sin \frac{\pi}{2}\right) \rightarrow (-12(0), -12(1))$

d) $(0, -12)$

A 4) Find four unique polar coordinates for each point given as rectangular coordinates.

Use $-360^\circ \leq \theta \leq 360^\circ$. Round to the nearest thousandths.

a) $(-1, 5)$ $r = \sqrt{1^2 + 5^2} = \sqrt{26}$
 $\theta = \tan^{-1}\left(\frac{5}{-1}\right) = -78.69 + 180^\circ = 101.309^\circ$

Q4 b) $(3, -7)$ $r = \sqrt{3^2 + (-7)^2} = \sqrt{58}$ Q4
 $\theta = \tan^{-1}\left(\frac{-7}{3}\right) = -66.801^\circ + 360^\circ$
 $\theta = 293.198^\circ$

a) $(\sqrt{26}, 101.309^\circ)$ $(\sqrt{26}, -258.691^\circ)$
 $(-\sqrt{26}, 281.309^\circ)$ $(-\sqrt{26}, -78.691^\circ)$

b) $(\sqrt{58}, 293.198^\circ)$ $(\sqrt{58}, -66.802^\circ)$
 $(-\sqrt{58}, 113.198^\circ)$ $(-\sqrt{58}, -246.802^\circ)$

Use $-2\pi \leq \theta \leq 2\pi$. Round to the nearest thousandths.

Q3 c) $(-5\sqrt{3}, -5)$ $r = \sqrt{(-5\sqrt{3})^2 + (-5)^2} = \sqrt{100}$ d) $(4, 3)$ $r = \sqrt{4^2 + 3^2} = 5$
 $r = 10$ $\theta = \tan^{-1}\left(\frac{3}{4}\right) = 0.643$
 $\theta = \tan^{-1}\left(\frac{-5}{-5\sqrt{3}}\right) = 0.524 + \pi = 3.665$

c) $(10, 3.665)$ $(10, -2.618)$
 $(-10, 0.524)$ $(-10, -5.760)$

d) $(5, 0.644)$ $(5, -5.640)$
 $(-5, 3.785)$ $(-5, -2.498)$