

9.01: Review of Measures of Center and Spread

median⁴
↓

1 2 4 9 100 111 22 5 6
1 2 (4 6) 12 15

3 MEASURES OF CENTRAL TENDENCY		
Mean	Median	Mode
<p>Denoted as \bar{x}, "x-bar" the average</p> <p>Sum of all the values \rightarrow $\bar{x} = \frac{\sum x}{n}$ \leftarrow # of terms</p>	<p>The number in the middle when the data is arranged in ascending order.</p> <p>If there are 2 numbers in the middle, then find their average.</p>	<p>The number which <u>occurs most frequently</u>. There does not have to be a mode. There can be more than one mode.</p> <p>Bimodal - 2 modes Trimodal - 3 modes</p>

Example 1: Given scores from the latest test: 90, ~~89~~, ~~78~~, ~~81~~, 68, 100, ~~84~~, ~~83~~, ~~83~~, 74, ~~88~~, ~~80~~, ~~73~~, 89, ~~82~~

a) Find the measures of central tendency. Don't forget to put the data in ascending order!!!

$n = 15$

$\frac{1192}{15} =$

32 68 73 74 78 80 81 83 83 84 88 89 89 90 100

↓
↑
↓

Q1 (74)
Q2
Q3 (89)

Mean: 79.47 Median: 83 Mode: 83, 89

5 NUMBER SUMMARY				
Minimum (Lower Extreme)	Lower (1st) Quartile Q_1	Median (2nd Quartile) Q_2	Upper (3rd) Quartile Q_3	Maximum (Upper Extreme)
Smallest number	The median of the lower half. If there are 2 numbers find their average.	Divides the data into a lower and upper half.	The median of the upper half. If there are 2 numbers find their average.	Largest number

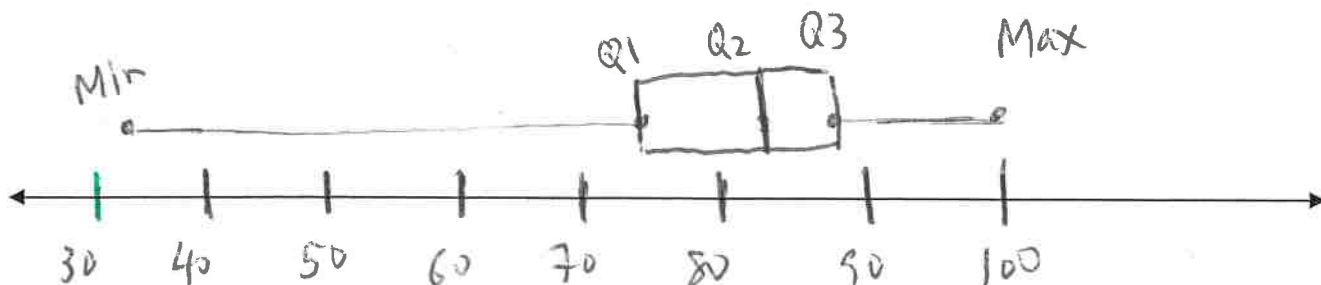
b) Find the 5-Number Summary of the test data above.

Min: 32 Q_1 : 74 Median: 83 Q_3 : 89 Max: 100

Box and Whisker Plot - A plot that displays the 5 number summary:

1. Draw a number line and scale it appropriately. Keep the minimum and maximum in mind.
2. Place points above the number line for each number in the 5 number summary.
3. Connect the minimum and Q_1 with a segment as well as Q_3 and the maximum.
4. Draw a box from Q_1 to Q_3 .
5. Draw a vertical segment through the median.

c) Draw a box and whisker plot for the previous test data.



SHAPE OF A BOX AND WHISKER PLOT		
Symmetric	Skewed Left	Skewed Right
mean = median	mean < median	mean > median

MEASURES OF DISPERSION (SPREAD)		
Range	Interquartile Range	Mean Absolute Deviation
The difference in the <u>maximum</u> and the <u>minimum</u> . (Max - Min)	The difference in the <u>upper quartile</u> and <u>lower quartile</u> . ($Q_3 - Q_1$) $Q_3 = 89$ $Q_1 = 74$	$MAD = \frac{\sum x_i - \bar{x} }{n}$ <i>mean = 79.47</i>

d) Find the measures of spread for the given data set of test scores.

Range = 68 IQR = 15 MAD = _____

$MAD = \frac{144.65}{15}$

MAD = 9.64

$100 - 32 =$

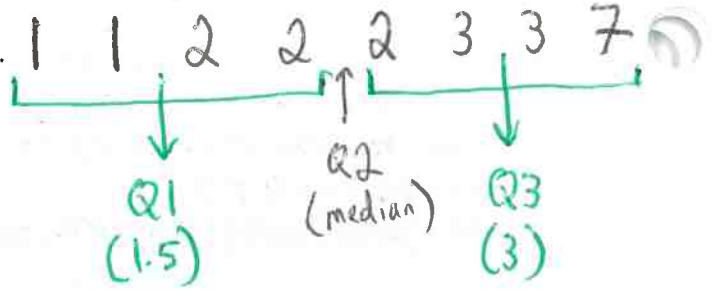
x	\bar{x}	$x - \bar{x}$
90	79.47	10.53
89	79.47	9.53
78	79.47	1.47
81	79.77	1.53
68	79.47	11.47

x	\bar{x}	$x - \bar{x}$
100	79.47	20.53
84	↓	4.53
83	↓	3.53
83	↓	3.53
74	↓	5.47
88	↓	8.53

x	\bar{x}	$x - \bar{x}$
80	79.47	0.53
73	↓	6.47
89	↓	9.53
32	↓	47.47

Example 2:

a) List the number of pets from 8 of your classmates.



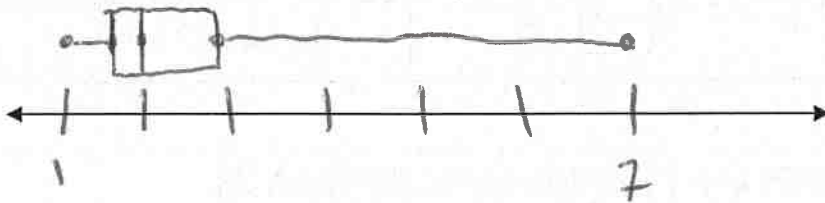
$$\bar{x} = \frac{21}{8} = 2.625$$

b) Calculate all measures of center, and the 5 number summary for the data.

$\bar{x} =$ 2.63 Median: 2 Mode: 2

Min: 1 Q1: 1.5 Median: 2 Q3: 3 Max: 7

c) Construct a box plot and describe the shape of the data.



Shape: skewed right

d) Calculate the measures of spread.

Range = $7 - 1 = 6$ IQR = $3 - 1.5 = 1.5$ MAD = 1.282

MAD

X	\bar{x}	$x - \bar{x}$	X	\bar{x}	$x - \bar{x}$
1	2.63	1.63	2	2.63	0.63
1	2.63	1.63	3	↓	0.37
2	2.63	0.63	3	↓	0.37
2	2.63	0.63	7	↓	4.37

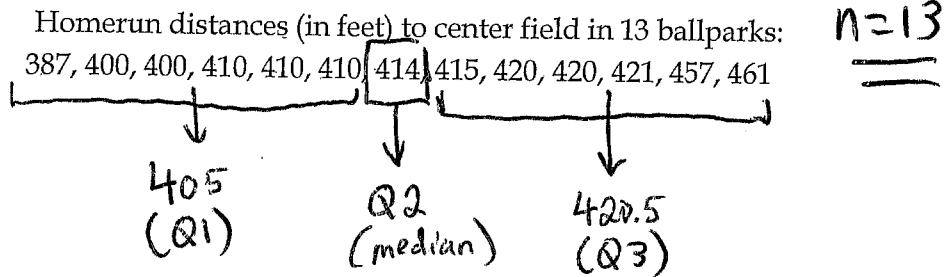
$$MAD = \frac{10.26}{8} = 1.282$$

BEST MEASURE OF CENTER AND SPREAD	
SYMMETRIC WITH NO OUTLIERS	SKEWED or WITH OUTLIERS
Mean and Mean Absolute Deviation (MAD)	Median and Interquartile Range (IQR)

9.01 Homework: Statistics Review

Date: _____

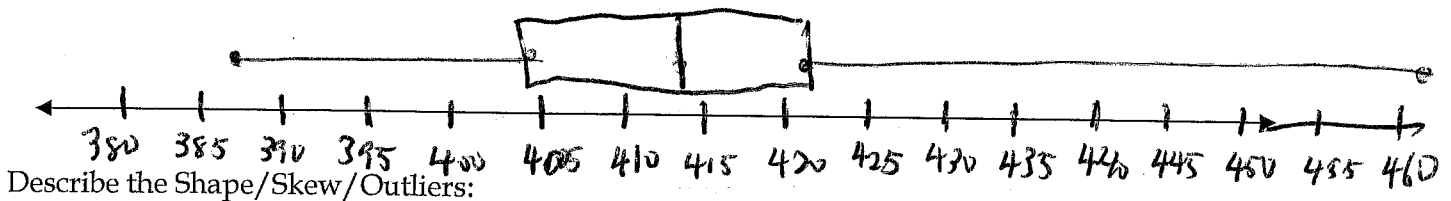
1. Calculate all measures of center, spread, and the 5 number summary for the data provided. Construct a box plot and describe the shape of the data. Indicate if there are any outliers.



$\bar{x} = 417.308$ Median: 414 Mode: 410

Min: 387 Q1: 405 Median: 414 Q3: 420.5 Max: 461

Range = $461 - 387 = 74$ IQR = $420.5 - 405 = 15.5$ MAD = 14.225



Skewed Right
outliers: 457, 461

2. Suppose that the numbers of unnecessary procedures recommended by five doctors in a 1-month period are 2, 2, 8, 10, and 18. If we ask a 6th doctor and find out that they recommend 35 procedures

(a) How will the Median and Mean be affected?

first 5: $\bar{x} = 8$
Median = 8

6 doctors:
 $\bar{x} = 12.5$
Median = 10

Both mean and median will both increase but mean increases by larger amount since data is skewed right.

(b) How will the IQR and Mean Absolute Deviation be affected?

IQR = 8
MAD = 4.8

IQR = 16
MAD = 9

Both IQR and MAD ~~both~~ increases by double the value.

3. Suppose the salaries (in dollars) of six employees are: 8000, 10000, 15000, 16000, 20000 and 39000.

Q2

a. What are the Median and Mean salaries?

Median: \$15,500

Mean: 18,000

b. Why are they such different numbers?

\$39,000 is an outlier that more significantly impacts the mean

c. Which measure of center is the better pick to describe this data? Why?

Median b/c it's less affected by the outlier

4. Based solely on the given mean and median, decide on the shape of each distribution (skewed left, skewed right, or approximately symmetric):

a. Mean = 100 Median = 98

close together

Shape: approximately symmetric

b. Mean = 20 Median = 41

mean significantly less

Shape: skewed left

c. Mean = 934 Median = 850

mean significantly more

Shape: skewed right