

**Accelerated Pre-Calculus  
May 2023 Calendar  
Units 10 - Logarithms**

Monday	Tuesday	Wednesday	Thursday	Friday
				4/28  Unit 10.01 (Day 1) Exponential Function Review  Math EOC (Algebra) 8:20-11:45am
5/1  10.01 Exponential Function Review  (Day 2) Solving Equations with like bases	5/2  10.02 Log Functions  Converting between log form and exponential form • Special log bases Evaluate logs	5/3  10.03 Properties of Logs • Expanding Logs • Condensing Logs	5/4  10.03 Properties of Logs (Day 2)	5/5  10.04 Solving Equations (Lesson 3-4) Exponential Equations
8  10.05 Solving Log Equations (Lesson 3-4) • Log Equations	9  10.06 Solving Log and exponential Equations- Lumberjack Logs Activity	10  10.07 Review  Logs- Solving Equations and Properties	11  10.07 Review (day 2)  Logs- Solving Equations and Properties	12  10.08 Graphing Log Functions
15  10.09 Graphing Log Functions (Day 2)	16  10.10 Log Test Review (Day 1)	17  10.10 Log Test Review (Day 2)	18  10.10 Log Test Review (Day 3)	19  <b>10.11 Log Test</b>
22  Makeups and Recoveries	23  Makeups and Recoveries (Periods 1,2,3)  *Half-Day 8:20am -12:40pm	24  Makeups and Recoveries (Periods 4,5,6)  *Half-Day 8:20am -12:40pm	25  <b>Last Day of School</b> Makeups and Recoveries (Period 7)  *Half-Day 8:20am -12:40pm	26  Teacher Post-Planning Day

Logarithms:  $\log_b x = y$  if and only if  $b^y = x$

The **logarithm** of a positive number is the **power** of the **base** that produces that number.

**log N** : A logarithm whose **base** is 10 is called a **common logarithm**.

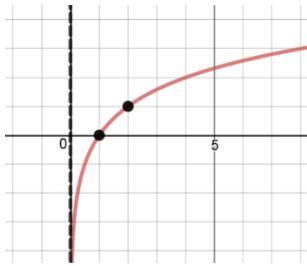
**ln N** : A logarithm whose **base** is e is called a **natural logarithm**.

### Properties of Logarithms:

- |                               |  |
|-------------------------------|--|
| (1) Argument = 1:             | $\log_b 1 = 0$ or $\log 1 = 0$ or $\ln 1 = 0$  |
| (2) Argument = Base:          | $\log_b b = 1$ or $\log 10 = 1$ or $\ln e = 1$                                       |
| (3) Argument = Power of Base: | $\log_b b^x = x$ or $\log 10^x = x$ or $\ln e^x = x$                                 |
| (4) Exponent = Logarithm:     | $b^{\log_b x} = x$ or $10^{\log x} = x$ or $e^{\ln x} = x$                           |
| (5) Product Property:         | $\log_b xy = \log_b x + \log_b y$  |
| (6) Quotient Property:        | $\log_b \frac{x}{y} = \log_b x - \log_b y$   |
| (7) Power Property:           | $\log_b x^m = m \log_b x$  |
| (8) One-to-One Property:      | $\log_b x = \log_b y$ if and only if $x = y$   |
| (9) Change of Base Property:  | $\log_b x = \frac{\log_a x}{\log_a b} = \frac{\log x}{\log b} = \frac{\ln x}{\ln b}$ |

### Graph of Logarithmic Function:

Parent Graph of  $f(x) = \log_2 x$



Function Transformation for  $g(x) = a \log_n(bx - h) + k$

- a is the vertical stretch (if  $|a| > 1$ ) or compression (if  $0 < |a| < 1$ )
- a is the reflection over the x-axis (if  $a < 0$ )
- b is the reflection over the y-axis (if  $b < 0$ )
- h is the horizontal shift (left if  $h < 0$  and right if  $h > 0$ )
- k is the vertical shift (up if  $k > 0$  and down if  $k < 0$ )

- (1) Graph the Asymptote:  $x = h$ , unless reflected over the y-axis then  $x = -h$ .
- (2) Find where the parent's x-intercept moved to by following the transformations.
- (3) Find where the additional point of (base, 1) moved to by following the transformations.
- (4) Draw a smooth curve approaching the asymptote.

Domain:  $(h, \infty)$ , unless reflected over the y-axis then  $(-\infty, -h)$

Range:  $(-\infty, \infty)$

For the new x-intercept: set  $g(x) = 0$  and solve for x.