

Ch. 5 Logs Review:

1. Find $f'(x)$ for $f(x) = \sqrt{\frac{(x+2)^3}{x(\sqrt[5]{2-7x})}}$

2. Find $\frac{d^2y}{dx^2}$ for $y = x(5^{1-6x})$

3. Find dy/dx for $f(x) = 3x^{(1-x)^2}$

4. $f(x) = 3x + 9x^{13}$ Find $(f^{-1})'(-12)$

5. Derive the derivative for $y = \operatorname{arcsec} x$ implicitly.

6. Find dy/dx for $y = \log_3 \left(\frac{1-x}{2x^2} \right) - 5e^{2x^2-5x} + \ln \left(\sqrt{(1-4x^2)^3} \right) - 9^{3-x-5x^2}$

7. Sketch the 6 Arc-trig graphs

Ch. 5 Logs Review:

Key

1. Find $f'(x)$ for $f(x) = \sqrt{\frac{(x+2)^3}{x(\sqrt[5]{2-7x})}}$ $\ln y = \ln \left[\frac{(x+2)^3}{x(\sqrt[5]{2-7x})} \right]^{1/2}$

$$\ln y = \frac{1}{2} \ln(x+2)^3 - \frac{1}{2} \ln x - \frac{1}{2} \ln(2-7x)^{1/5}$$

$$\ln y = \frac{3}{2} \ln(x+2) - \frac{1}{2} \ln x - \frac{1}{10} \ln(2-7x)$$

$$\frac{1}{y} \frac{dy}{dx} = \frac{3}{2} \left(\frac{1}{x+2} \right) - \frac{1}{2} \left(\frac{1}{x} \right) - \frac{1}{10} \left(\frac{-7}{2-7x} \right)$$

$$\frac{dy}{dx} = \sqrt{\frac{(x+2)^3}{x(\sqrt[5]{2-7x})}} \left[\frac{3}{2(x+2)} - \frac{1}{2x} + \frac{7}{10(2-7x)} \right]$$

2. Find $\frac{d^2y}{dx^2}$ for $y = x(5^{1-6x})$

$$\frac{dy}{dx} = 1 \cdot 5^{1-6x} + x \cdot \ln 5 \cdot 5^{(1-6x)} \cdot (-6) = 5^{1-6x} - 6x \ln 5 (5)^{1-6x}$$

$$\frac{d^2y}{dx^2} = \ln 5 \cdot 5^{(1-6x)} \cdot (-6) - 6 [\ln 5 \cdot 5^{1-6x}] - 6x \cdot \ln 5 \cdot \ln 5 \cdot 5^{1-6x} \cdot (-6)$$

$$= -6 \ln 5 \cdot 5^{(1-6x)} - 6 \ln 5 \cdot 5^{(1-6x)} + 36 (\ln 5)^2 x \cdot 5^{1-6x}$$

$$= -12 \ln 5 (5^{1-6x}) + 36 (\ln 5)^2 x \cdot 5^{(1-6x)}$$

3. Find dy/dx for $f(x) = 3x^{(1-x)^2}$

$$y = 3x^{(1-x)^2}$$

$$\ln y = \ln 3x^{(1-x)^2}$$

$$\ln y = \ln 3 + \ln x^{(1-x)^2}$$

$$\ln y = \ln 3 + (1-x)^2 \ln x$$

$$\frac{1}{y} \left(\frac{dy}{dx} \right) = 0 + 2(1-x)(-1) \ln x + (1-x)^2 \left(\frac{1}{x} \right)$$

$$\frac{dy}{dx} = 3x^{(1-x)^2} \left[2(x-1) \ln x + \frac{(1-x)^2}{x} \right]$$

$$f'(x) = 3 + 117x^{12}$$

$$f'(-1) = 3 + 117 = 120$$

4. $f(x) = 3x + 9x^{13}$ Find $(f^{-1})'(-12)$

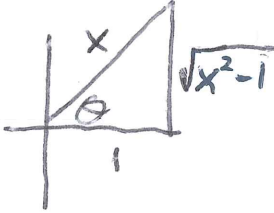
$$-12 = 3x + 9x^{13}$$

$$x = -1$$

$$f(-1) = -12 \mid (f^{-1})(-12) = -1$$

$$f'(-1) = \boxed{120} \mid (f^{-1})'(-12) = \boxed{\frac{1}{120}}$$

5. Derive the derivative for $y = \text{arcsec } x$ implicitly.

$$\sec y = \sec(\text{arcsec } x) \quad \left. \begin{aligned} \frac{dy}{dx} &= \frac{1}{\sec(\text{arcsec } x) \cdot \tan(\text{arcsec } x)} \\ \sec y &= x \\ \left(\frac{dy}{dx}\right) \sec y \tan y &= 1 \\ \frac{dy}{dx} &= \frac{1}{\sec y \tan y} \end{aligned} \right\} \frac{dy}{dx} = \frac{1}{|x| \sqrt{x^2 - 1}}$$


6. Find dy/dx for $y = \log_3 \left(\frac{1-x}{2x^2} \right) - 5e^{2x^2-5x} + \ln \left(\sqrt{(1-4x^2)^3} \right) - 9^{3-x-5x^2}$

$$y = \log_3(1-x) - \log_3(2x^2) - 5e^{2x^2-5x} + \frac{3}{2} \ln(1-4x^2) - 9^{(3-x-5x^2)}$$

$$y' = \frac{1}{\ln 3} \left(\frac{-1}{1-x} \right) - \frac{1}{\ln 3} \left(\frac{4x}{2x^2} \right) - 5e^{2x^2-5x} (4x-5) + \frac{3}{2} \left(\frac{-8x}{1-4x^2} \right) - \ln 9 \cdot 9^{3-x-5x^2} (-1-10x)$$

$$y' = \frac{-1}{\ln 3(1-x)} - \frac{4x}{(\ln 3)2x^2} - 5(4x-5)e^{2x^2-5x} - \frac{24x}{2(1-4x^2)} + (\ln 9)(1+10x)9^{(3-x-5x^2)}$$

7. Sketch the 6 Arc-trig graphs

