

BC Calculus - Unit 1 Test Review (Limits)

Evaluate the Limit

$$1) \lim_{x \rightarrow 0} \frac{\sqrt{x+19} - \sqrt{19}}{x}$$

$$2) \lim_{x \rightarrow -3} \frac{x+3}{x^2+2x-3}$$

$$3) \lim_{x \rightarrow 2^-} \frac{|x-2|}{x-2}$$

$$4) \lim_{x \rightarrow 0} \frac{\frac{1}{x+1} - 1}{x}$$

$$5) \lim_{x \rightarrow \infty} \frac{4x^5 - 2x^2 + 3}{3x^2 + 2x^5 - x^4}$$

$$6) \lim_{x \rightarrow \infty} x^5 3^{-x}$$

$$7) \lim_{x \rightarrow -3^-} \frac{x^2+3}{x+3}$$

$$8) \lim_{x \rightarrow 1^+} \frac{x^2+2x+1}{x-1}$$

9) Let g and h be the functions defined by $g(x) = -\frac{1}{4}x^2 - \frac{1}{2}x - \frac{9}{4}$ and $h(x) = \sin\left(\frac{\pi}{2}x\right) - 1$. If f is a function that satisfies $g(x) \leq f(x) \leq h(x)$ for all x , what is $\lim_{x \rightarrow -1} f(x)$?

10) Let f be the function defined by $f(x) = \begin{cases} \frac{x^2+8x+12}{x+6}, & x \neq -6 \\ b, & x = -6 \end{cases}$. For what value of b is f continuous at $x = -6$? (support answer with continuity conditions)

Give the value of each statement. If the value does not exist, write “does not exist” or “undefined.”

11. $\lim_{x \rightarrow 3} f(x) =$

15. $\lim_{x \rightarrow 2} f(x) =$

12. $\lim_{x \rightarrow 1} f(x) =$

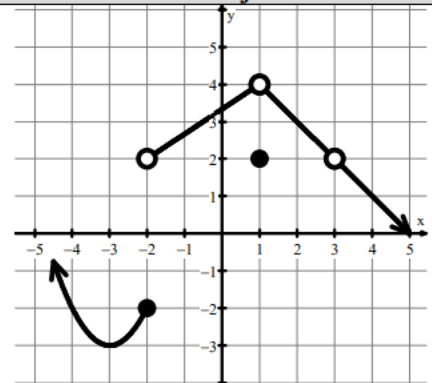
16. $\lim_{x \rightarrow -2^+} f(x) =$

13. $f(3) =$

17. $f(1) =$

14. $f(-2) =$

18. $\lim_{x \rightarrow -2^-} f(x) =$



19) If $f(x) = \begin{cases} \sin x, & x < -\pi \\ \tan x & -\pi < x < \frac{\pi}{4} \\ \cos x, & x \geq \frac{\pi}{4} \end{cases}$, find the following:

a. $\lim_{x \rightarrow -\pi^-} f(x) =$

b. $\lim_{x \rightarrow -\pi} f(x) =$

c. $\lim_{x \rightarrow \frac{\pi}{4}} f(x) =$

d. $f\left(\frac{\pi}{4}\right) =$

20) If $f(x) = \frac{x+3}{x^2-2x-15}$, identify the type of each discontinuity and where it is located.

21) Identify all horizontal asymptotes of $f(x) = \frac{\sqrt{16-x^3+5x}}{5x^3-8x}$

22)

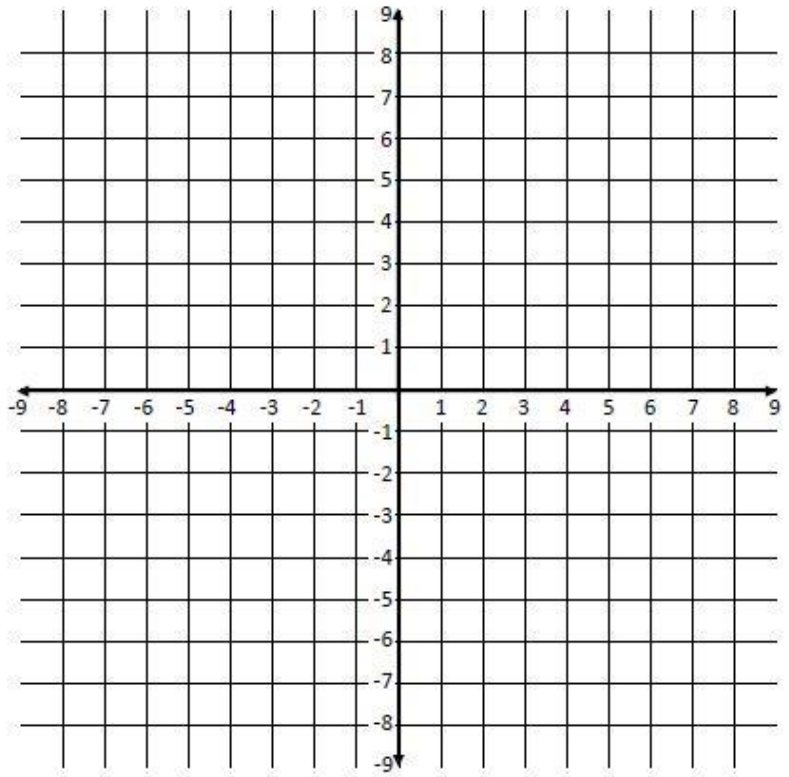
$$g(x) = \begin{cases} \frac{x+5}{2x-4}, & x < 2 \\ 12, & x = 2 \\ 2x - 5, & 2 < x < 5 \\ 20, & x = 5 \\ \frac{-x^2+4}{5-x}, & x > 5 \end{cases}$$

Find the following :

a) $\lim_{x \rightarrow -\infty} g(x) =$	b) $\lim_{x \rightarrow 2^-} g(x) =$	c) $\lim_{x \rightarrow 2^+} g(x) =$
d) $\lim_{x \rightarrow 2} g(x) =$	e) $\lim_{x \rightarrow 5^-} g(x) =$	f) $\lim_{x \rightarrow 5^+} g(x) =$
g) $\lim_{x \rightarrow 5} g(x) =$	h) $\lim_{x \rightarrow 3^+} g(x) =$	i) $\lim_{x \rightarrow \infty} g(x) =$

23) On the coordinate plane below, sketch a **function graph** with the following characteristics:

- a. $\lim_{x \rightarrow -\infty} f(x) = 8$
- b. $f(-6) = -3$
- c. $\lim_{x \rightarrow -6} f(x) = 4$
- d. $\lim_{x \rightarrow -2} f(x) = \infty$
- e. $f(3) = 7$
- f. $\lim_{x \rightarrow 3} f(x)$ does not exist
- g. $\lim_{x \rightarrow 3^+} f(x) = 5$
- h. $\lim_{x \rightarrow \infty} f(x) = -\infty$



24) Find the value of **k** which makes the following piecewise function continuous for all values of **x**. (Use continuity conditions to justify)

$$f(x) = \begin{cases} 2x + k & \text{if } x \leq -2 \\ kx - 3 & \text{if } x > -2 \end{cases}$$

25) a) Verify Intermediate Value Theorem (IVT) applies to $f(x) = \frac{x^2+x}{x-1}$ on $\left[\frac{5}{2}, 4\right]$ for $f(c) = 6$

b) Find c-value