

Essential Questions: How do we classify polygons?
What are the steps to finding the measure of interior and exterior angles of a polygon?

A _____ is a plane figure that meets the following conditions:

a.

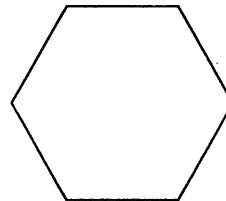
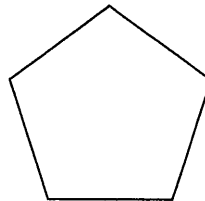
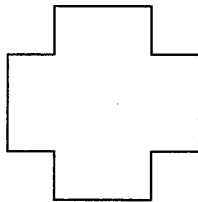
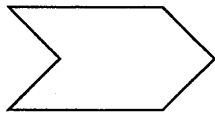
b.

Vertex-

Concave polygon-

Convex polygon-

Examples: Which polygons are convex/concave:



Equilateral polygon-

Equiangular polygon-


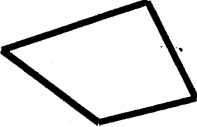
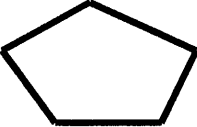
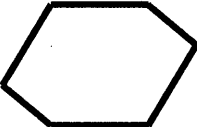
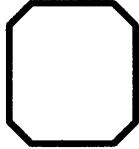
Regular polygon-

Fill in the chart below.

Number of Sides	Name of Polygon	Number of Sides	Name of Polygon
3			Octagon
	Quadrilateral	9	
	Pentagon		Decagon
6		12	
	Heptagon	n	

Recall: The three angles of a triangle _____

Diagonal-

Polygon	Diagram	Number of Sides	Number of Triangles Made from Diagonals	Sum of the measures of the Interior Angles
Triangle				
Quadrilateral				
Pentagon				
Hexagon				
Octagon				
n-gon				

If a polygon has n sides, how many triangles can be drawn inside it using diagonals drawn from one vertex? _____

If a polygon has n sides, what is the sum of the measures of its interior angles?

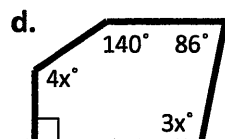
Examples: Find the sum of the measures of the interior angles of a ...

a. ... Nonagon

b. ... 14-gon

c. ... 37-gon

Find the value of x .



Examples: The sum of the measures of the interior angles of a polygon is given. Classify the polygon by the number of sides.

e. 900°

Examples: Find the measure of one interior angle of each regular polygon. One angle =

h. hexagon

i. octagon

j. 20-gon

Example: One interior angle of a regular polygon is given. Find the number of sides.

f. 108°

g. 120°

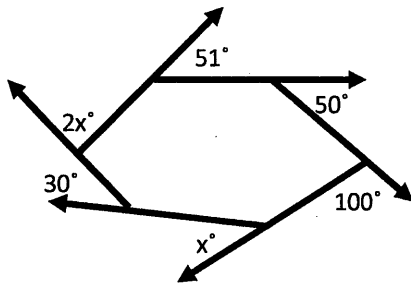
The **exterior angles** of a polygon can be dilated together to all fit around a single point, no matter how many sides the polygon has.

<http://www.geogebra.org/material/simple/id/152420>

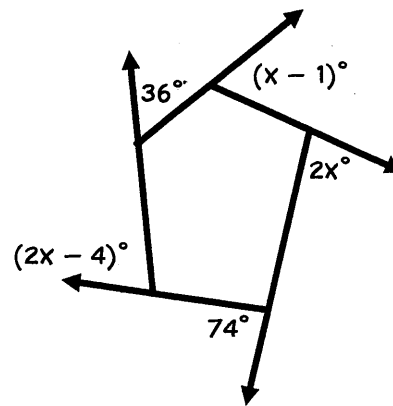
If a polygon has n sides, what is the sum of the measures of the exterior angles?

Examples:

k.



l.



Examples: Find the measure of one exterior angle of each regular polygon. One angle =

m. heptagon

n. decagon

6-1 Skills Practice**Angles of Polygons**

Find the sum of the measures of the interior angles of each convex polygon.

1. nonagon

2. heptagon

3. decagon

The measure of an interior angle of a regular polygon is given. Find the number of sides in the polygon.

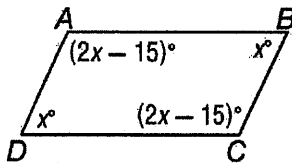
4. 108

5. 120

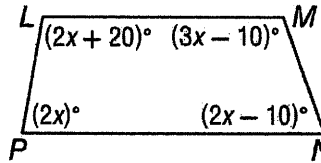
6. 150

Find the measure of each interior angle.

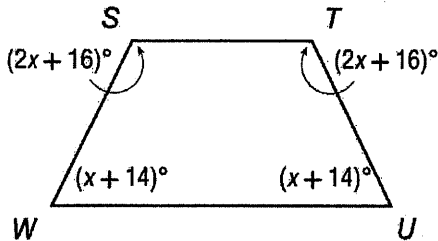
7.



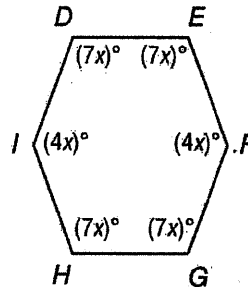
8.



9.



10.



Find the measures of each interior angle of each regular polygon.

11. quadrilateral

12. pentagon

13. Dodecagon

Find the measures of each exterior angle of each regular polygon.

14. octagon

15. nonagon

16. 12-gon

Key

Essential Questions: How do we classify polygons?

What are the steps to finding the measure of interior and exterior angles of a polygon?

A polygon is a plane figure that meets the following conditions:

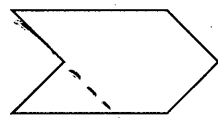
- a. formed by 3 or more segments called sides such that no 2 sides with a common endpoint are collinear (not along same line)
- b. each side intersects exactly 2 other sides, one at each endpoint.

Vertex- endpoint of a side

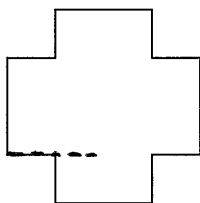
Concave polygon- not convex - a line containing a side contains a point in the interior

Convex polygon- no line that contains a side contains a point in the interior of the polygon.

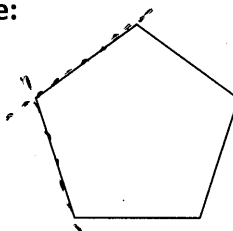
Examples: Which polygons are convex/concave:



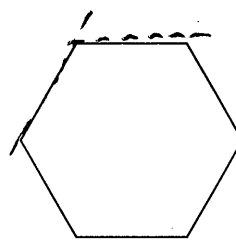
concave



concave



convex



convex

Equilateral polygon- all sides are congruent

Equiangular polygon- all angles are congruent

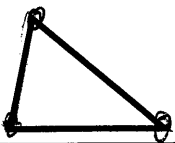
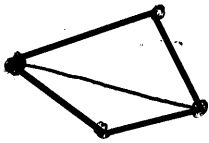
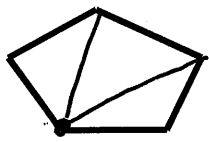
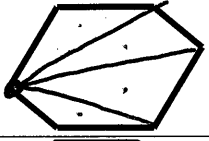
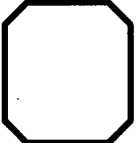
Regular polygon- all sides are congruent (\cong) and all angles congruent ($\angle's \cong$)

Fill in the chart below.

Number of Sides	Name of Polygon	Number of Sides	Name of Polygon
3	triangle	8	Octagon
4	Quadrilateral	9	nonagon
5	Pentagon	10	Decagon
6	hexagon	12	dodecagon
7	Heptagon	n	n-gon

Recall: The three angles of a triangle add to be 180°

Diagonal-

Polygon	Diagram	Number of Sides	Number of Triangles Made from Diagonals	Sum of the measures of the Interior Angles
Triangle		3	1	180°
Quadrilateral		4	2	360°
Pentagon		5	3	540°
Hexagon		6	4	720°
Octagon		8	6	1080°
n-gon		n	$n-2$	$180(n-2)$

If a polygon has n sides, how many triangles can be drawn inside it using diagonals drawn from one vertex? $n-2$

If a polygon has n sides, what is the sum of the measures of its interior angles?

$$180(n-2)$$

Examples: Find the sum of the measures of the interior angles of a ...

a. ... Nonagon $n = 9$

b. ... 14-gon $n = 14$

c. ... 37-gon

$$180(9-2) = 1260^\circ$$

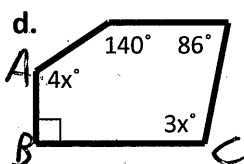
$$180(12) = 2160^\circ$$

$$180(n-2)$$

$$180(35)$$

$$6300^\circ$$

Find the value of x .



$$n = 5$$

$$180(n-2)$$

$$180(3) = 540^\circ$$

$$\angle A = 4(32) = 128^\circ$$

$$\angle C = 3(32) = 96^\circ$$

$$7x + 140^\circ + 86^\circ + 90^\circ = 540$$

$$7x + 316 = 540$$

$$7x = 224$$

$$\boxed{x = 32}$$

Examples: The sum of the measures of the interior angles of a polygon is given. Classify the polygon by the number of sides.

e. 900°

$$\begin{array}{l} \text{Sum} = 180(n-2) \\ 900 = 180(n-2) \\ \frac{900}{180} = \frac{180(n-2)}{180} \\ 5 = n-2 \\ +2 \quad +2 \\ \boxed{7 = n} \end{array} \quad \frac{900}{7} = 128.57$$

Examples: Find the measure of one interior angle of each regular polygon. One angle = $\frac{180(n-2)}{n}$

h. hexagon $n=6$

$$\frac{180(6-2)}{6} = \boxed{120^\circ}$$

i. octagon $n=8$

$$\frac{180(8-2)}{8} = \boxed{135^\circ}$$

j. 20-gon

$$\frac{180(18)}{20} = \boxed{162^\circ}$$

Example: One interior angle of a regular polygon is given. Find the number of sides.

f. 108°

$$\frac{108}{1} = \frac{180(n-2)}{n}$$

$$108n = 180(n-2)$$

$$108n = 180n - 360$$

$$-180n \quad -180n$$

$$-72n = -360$$

$$\frac{-72n}{-72} = \frac{-360}{-72}$$

$$\boxed{n = 5}$$

The **exterior angles** of a polygon can be dilated together to all fit around a single point, no matter how many sides the polygon has.

<http://www.geogebra.org/material/simple/id/152420>

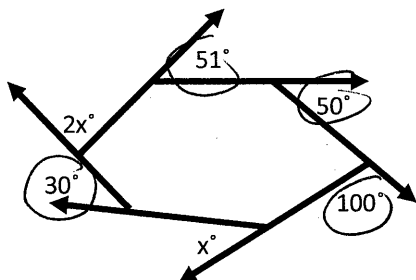
If a polygon has n sides, what is the sum of the measures of the exterior angles?

$$\text{Sum} = 360^\circ$$

Examples:

$$\text{Sum} = 360$$

k.



$$3x + 30 + 51 + 50 + 100 = 360$$

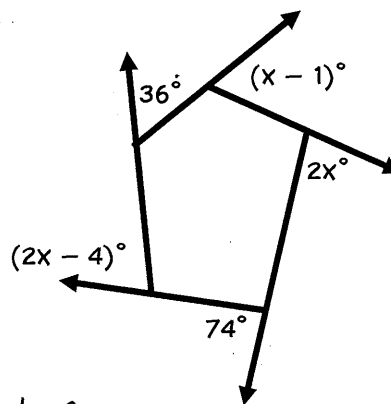
$$3x + 231 = 360$$

$$-231 \quad -231$$

$$3x = 129$$

$$\boxed{x = 43}$$

l.



$$36 + x - 1 + 2x + 74 + 2x - 4 = 360$$

$$5x + 105 = 360$$

$$5x = 255$$

$$\boxed{x = 51}$$

Examples: Find the measure of one exterior angle of each regular polygon. One angle = $\frac{360}{n}$

m. heptagon $n=7$

$$\frac{360}{7} = \boxed{51.429^\circ}$$

n. decagon $n=10$

$$\frac{360}{10} = \boxed{36^\circ}$$

6-1 Skills Practice

Angles of Polygons

Find the sum of the measures of the interior angles of each convex polygon.

1. nonagon $7 \cdot 180$

1260°

2. heptagon $5 \cdot 180$

900°

3. decagon $8 \cdot 180$

1440°

The measure of an interior angle of a regular polygon is given. Find the number of sides in the polygon. $\frac{180(n-2)}{n}$

4. 108 $\frac{108n}{1} = \frac{180(n-2)}{n}$

$108n = 180n - 360$
 $-72n = -360$ $n = 5$

5. 120 $\frac{120n}{1} = \frac{180(n-2)}{n}$

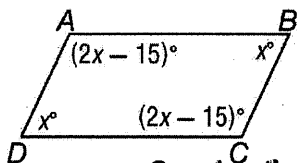
$120n = 180n - 360$
 $-60n = -360$
 $n = 6$

6. 150 $\frac{150n}{1} = \frac{180(n-2)}{n}$

$150n = 180n - 360$
 $-30n = -360$ $n = 12$

Find the measure of each interior angle.

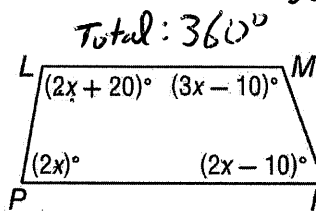
7.



$4x - 30 + 2x = 360$
 $6x = 390$
 $x = 65$

$\angle A = 115^\circ$ $\angle B = 65^\circ$
 $\angle D = 65^\circ$ $\angle C = 115^\circ$

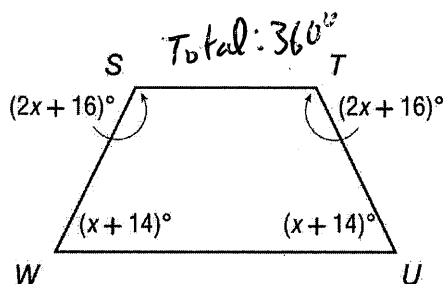
8.



$9x = 360$
 $x = 40$

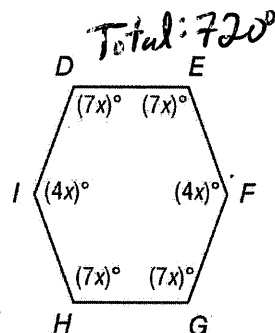
$\angle L = 100^\circ$ $\angle M = 110^\circ$
 $\angle P = 80^\circ$ $\angle N = 70^\circ$

9.



$6x + 60 = 360$
 $6x = 300$
 $x = 50$
 $\angle S = 116^\circ$ $\angle T = 116^\circ$
 $\angle W = 64^\circ$ $\angle U = 64^\circ$

10.



$36x = 720$ $x = 20$
 $\angle D = 140^\circ$ $\angle E = 140^\circ$
 $\angle I = 80^\circ$ $\angle F = 80^\circ$
 $\angle H = 140^\circ$ $\angle G = 140^\circ$

Find the measures of each interior angle of each regular polygon.

11. quadrilateral $n=4$

$\frac{360}{4} = 90^\circ$

12. pentagon $n=5$

$\frac{540}{5} = 108^\circ$

13. Dodecagon $n=12$

$\frac{180 \cdot 10}{12} = 150^\circ$

Find the measures of each exterior angle of each regular polygon.

14. octagon n

$\frac{360}{8} = 45^\circ$

15. nonagon

$\frac{360}{9} = 40^\circ$

16. 12-gon

$\frac{360}{12} = 30^\circ$