

Given $x^2y + y^2 = 2x$, differentiate with respect to t .

Steps: 1) Find each variable's derivative. 2) Instead of attaching $\frac{dy}{dx}$ to y 's derivative, now you will attach $\frac{dx}{dt}$ to x 's derivative and $\frac{dy}{dt}$ to y 's derivative.

* apply product rule, implicit differentiation

$$\overbrace{x^2}^{f \cdot g} y + y^2 = 2x$$

$$\overbrace{2x}^{f'} \overbrace{\left(\frac{dx}{dt}\right)}^{g'} y + \overbrace{x^2}^{f \cdot g} \overbrace{\left(\frac{dy}{dt}\right)}^{g'} + 2y \left(\frac{dy}{dt}\right) = 2 \left(\frac{dx}{dt}\right)$$

Answer