

All official participants must take this contest at the same time.

Contest Number 4 *Any calculator without a QWERTY keyboard is allowed. Answers must be exact or have 4 (or more) significant digits, correctly rounded.* January 5, 2021

Name \_\_\_\_\_ Teacher \_\_\_\_\_ Grade Level \_\_\_\_\_ Score \_\_\_\_\_

Time Limit: 30 minutes

NEXT CONTEST: FEB. 9, 2021

Answer Column

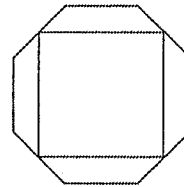
4-1. What is the smallest composite number which is the sum of two different prime numbers?

4-1.

4-2. If the lengths of the sides of right triangle T are  $3^2$ ,  $4^2$ , and  $y$ , what are both possible values of  $y$ ?

4-2.

4-3. What is the perimeter of a square whose vertices, as shown, are mid-points of alternating sides of a regular octagon whose perimeter is  $16\sqrt{2}$ ?

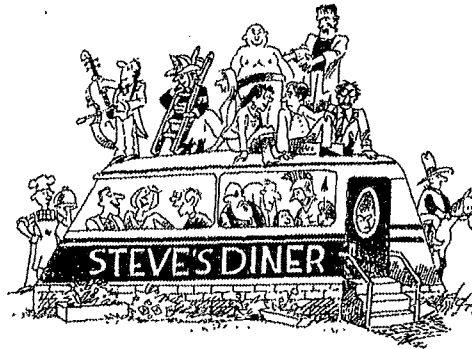


4-3.

4-4. Of the positive integers less than 2021, how many can be written as a difference of two powers of 2?

4-4.

4-5. What is the least number  $n$  with the property that, in every group of  $n$  people, there are at least three people who are all friends (each knows the other two) or all strangers (none of them knows either of the other two)?



4-5.

4-6. The numbers 12, 34, 56, 78, 90 are five two-digit numbers that use all ten digits. Which five two-digit numbers that use all ten digits have the largest possible product?

4-6.

Twenty-one books of past contests, *Grades 4, 5, & 6 (Volumes 1-7)*, *Grades 7 & 8 (Volumes 1-7)*, and *HS (Volumes 1-7)*, are available, for \$12.95 each volume (\$15.95 Canadian), from Math League Press, P.O. Box 17, Tenafly, NJ 07670-0017.