

1) Find $\frac{f(x+\Delta x)-f(x)}{\Delta x}$ for $f(x) = 2x - 5$

2) Find $\frac{f(x+\Delta x)-f(x)}{\Delta x}$ for $f(x) = 1 - x + 2x^2$

3) Find $\frac{f(x)-f(2)}{x-2}$ for $f(x) = 7x^2 + 1$

4) Find $f(x - 3) - f(x)$ for $f(x) = 5 - 6x$

5) Find $\frac{f(x+h)-f(x)}{h}$ for $f(x) = 3 - 2x^2$

6) Find $\frac{f(x+h)-f(x)}{h}$ for $f(x) = \sqrt{2x - 1}$

1) Find $\frac{f(x+\Delta x) - f(x)}{\Delta x}$ for $f(x) = 2x - 5$

$$f(x) = 2(x) - 5$$

$$f(x+\Delta x) = 2(x+\Delta x) - 5$$

$$f(x+\Delta x) = 2(x+\Delta x) - 5$$

$$\frac{2(x+\Delta x) - 5 - (2x - 5)}{\Delta x}$$

$$\frac{2x + 2\Delta x - 5 - 2x + 5}{\Delta x}$$

$$\frac{2\Delta x}{\Delta x} = \boxed{2}$$

2) Find $\frac{f(x+\Delta x) - f(x)}{\Delta x}$ for $f(x) = 1 - (x) + 2x^2$

$$f(x) = 1 - (x) + 2(x)^2$$

$$f(x+\Delta x) = 1 - (x+\Delta x) + 2(x+\Delta x)^2$$

$$\frac{1 - (x+\Delta x) + 2(x+\Delta x)^2 - (1 - x + 2x^2)}{\Delta x}$$

$$\frac{1 - x - \Delta x + 2(x^2 + 2x\Delta x + \Delta x^2) - 1 + x - 2x^2}{\Delta x}$$

$$\frac{\cancel{1} - \cancel{x} - \Delta x + \cancel{2x^2} + 4x\Delta x + 2\Delta x^2 - \cancel{1} + \cancel{x} - \cancel{2x^2}}{\Delta x}$$

$$\frac{-\Delta x + 4x\Delta x + 2\Delta x^2}{\Delta x}$$

$$\frac{\cancel{\Delta x}(-1 + 4x + 2\Delta x)}{\cancel{\Delta x}}$$

$$\boxed{-1 + 4x + 2\Delta x}$$

3) Find $\frac{f(x) - f(2)}{x - 2}$ for $f(x) = 7x^2 + 1$

$$f(2) = 7(2)^2 + 1 = 29$$

$$\frac{7x^2 + 1 - 29}{x - 2} \rightarrow \frac{7x^2 - 28}{x - 2}$$

$$\frac{7(x^2 - 4)}{x - 2} \rightarrow \frac{7(x+2)(\cancel{x-2})}{(x\cancel{-2})} \rightarrow \boxed{7(x+2)}$$

or

$$\boxed{7x + 14}$$

4) Find $f(x-3) - f(x)$ for $f(x) = 5 - 6x$

$$\begin{array}{l|l} f(\quad) = 5 - 6(\quad) & 23 - 6x - (5 - 6x) \\ f(x-3) = 5 - 6(x-3) & 23 - \cancel{6x} - 5 + \cancel{6x} \\ = 5 - 6x + 18 & \\ f(x-3) = 23 - 6x & \boxed{18} \end{array}$$

5) Find $\frac{f(x+h) - f(x)}{h}$ for $f(x) = 3 - 2x^2$

$$\begin{array}{l|l|l} f(\quad) = 3 - 2(\quad)^2 & \frac{3 - 2(x+h)^2 - (3 - 2x^2)}{h} & \frac{\cancel{3} - 2x^2 - 4xh - 2h^2 - \cancel{3} + 2x^2}{h} \\ f(x+h) = 3 - 2(x+h)^2 & \frac{3 - 2(x^2 + 2xh + h^2) - 3 + 2x^2}{h} & \frac{\cancel{h}(-4x - 2h)}{\cancel{h}} \\ & & \boxed{-4x - 2h} \end{array}$$

6) Find $\frac{f(x+h) - f(x)}{h}$ for $f(x) = \sqrt{2x-1}$

$$\begin{array}{l|l} f(\quad) = \sqrt{2(\quad) - 1} & \frac{\sqrt{2(x+h) - 1} - \sqrt{2x - 1}}{h} \\ f(x+h) = \sqrt{2(x+h) - 1} & \boxed{\frac{\sqrt{2x+2h-1} - \sqrt{2x-1}}{h}} \end{array}$$