

Solve for x by Factoring

1) $10x^3 = 28x^2 + 6x$

2) $32x = 50x^3$

Factored Form: _____

Factored Form: _____

Solution: _____

Solution: _____

3) Identify any intercepts (if any) and test for symmetry $y^2 = x^4 - 9$

4) x-intercept(s): _____ y-intercept: _____ Symmetry: _____

4) Identify the type(s) of symmetry for: $5x^4y^4 + 3x^7y^3 - 12x = 0$

5) Find the point(s) of intersection (ordered pairs!) of the graphs of the equations:

$$x^2 + y^2 = 5$$

$$3x - y = 5$$

Slope $m = \frac{y_2 - y_1}{x_2 - x_1}$

slope-intercept form: $y = mx + b$

point-slope form: $y - y_1 = m(x - x_1)$

- 6) Find an equation of the line (point-slope form) that passes through the points $(-1, -6)$ and $(2, 5)$
- 7) Find an equation of the line (point-slope form) containing the point $(-1, 5)$ that is parallel to the line $-2x + 3y = 19$
- 8) Find an equation of the line (point-slope form) containing the point $(-5, 1)$ that is perpendicular to the line $5x - 4y + 13 = 0$
- 9) Write an equation of the line that passes through $(-3, 7)$ and is perpendicular to the line $x = 1$
- 10) Write an equation of the line that passes through $(2, -4)$ and is parallel to the line $y = -2$

Key

Solve for x by Factoring

1) $10x^3 = 28x^2 + 6x$

$$10x^3 - 28x^2 - 6x = 0$$

$$2x(5x^2 - 14x - 3) = 0$$

$$2x(x-3)(5x+1) = 0$$

$$\begin{array}{r} -15 \\ 5 \overline{) -15} \\ \underline{5} \\ -14 \\ \underline{-14} \\ 0 \end{array}$$

Factored Form: $2x(x-3)(5x+1)$

Solution: $x = 0, 3, -1/5$

2) $32x = 50x^3$

$$32x - 50x^3 = 0$$

$$2x(16 - 25x^2) = 0$$

$$\begin{array}{cc} \wedge & \wedge \\ 4 & 4 & 5x & 5x \end{array}$$

$$2x(4-5x)(4+5x) = 0$$

$$\begin{array}{l} 4-5x=0 \\ 4=5x \end{array}$$

Factored Form: $2x(4-5x)(4+5x)$

Solution: $x = 0, 4/5, -4/5$

3) Identify any intercepts (if any) and test for symmetry $y^2 = x^4 - 9$

$$0 = x^4 - 9$$

$$\begin{array}{cc} \wedge & \wedge \\ x^2 & x^2 & 3 & 3 \end{array}$$

$$y^2 = 0^4 - 9$$

$$\sqrt{y^2} = \sqrt{-9}$$

none

$$0 = (x^2 - 3)(x^2 + 3)$$

x-intercept(s): $x = \pm\sqrt{3}$ y-intercept: none Symmetry: x-axis, y-axis
 set $y=0$ $(\sqrt{3}, 0), (-\sqrt{3}, 0)$ set $x=0$

4) Identify the type(s) of symmetry for: $5x^4y^4 + 3x^7y^3 - 12x = 0$

none

5) Find the point(s) of intersection (ordered pairs!) of the graphs of the equations:

$$x^2 + y^2 = 5$$

$$3x - y = 5$$

$$3x - 5 = y$$

$$x^2 + (3x-5)^2 = 5$$

$$x^2 + (3x-5)(3x-5) = 5$$

$$x^2 + 9x^2 - 15x - 15x + 25 = 5$$

$$10x^2 - 30x + 20 = 0$$

$$10(x^2 - 3x + 2) = 0$$

$$10(x-2)(x-1) = 0$$

$$x-2=0 \quad | \quad x-1=0$$

$$x=2 \quad | \quad x=1$$

$$* y = 3x - 5$$

$$y = 3(2) - 5$$

$$y = 6 - 5 = 1$$

(2, 1)

$$y = 3x - 5$$

$$y = 3(1) - 5 = -2$$

(1, -2)

Slope $m = \frac{y_2 - y_1}{x_2 - x_1}$

slope-intercept form: $y = mx + b$

point-slope form: $y - y_1 = m(x - x_1)$

- 6) Find an equation of the line (point-slope form) that passes through the points $(-1, -6)$ and $(2, 5)$

slope: $m = \frac{5 - (-6)}{2 - (-1)} = \frac{11}{3}$ point: $(2, 5)$ slope: $m = \frac{11}{3}$

$$y - 5 = \frac{11}{3}(x - 2)$$

or $y + 6 = \frac{11}{3}(x + 1)$

- 7) Find an equation of the line (point-slope form) containing the point $(-1, 5)$ that is parallel to the line $-2x + 3y = 19$

$$3y = 2x + 19$$

$$y = \frac{2}{3}x + \frac{19}{3}$$

$$m = \frac{2}{3}$$

point: $(-1, 5)$

slope: $m = \frac{2}{3}$

$$y - 5 = \frac{2}{3}(x + 1)$$

- 8) Find an equation of the line (point-slope form) containing the point $(-5, 1)$ that is perpendicular to the line $5x - 4y + 13 = 0$

$$5x - 4y + 13 = 0$$

$$-4y = -5x - 13$$

$$y = \frac{-5x}{-4} - \frac{13}{-4}$$

$$y = \frac{5}{4}x + \frac{13}{4}$$

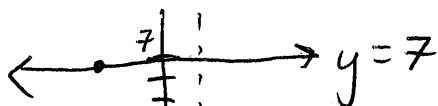
$$m_1 = \frac{5}{4}$$

$$m_2 = -\frac{4}{5}$$

point: $(-5, 1)$ slope: $m = -\frac{4}{5}$

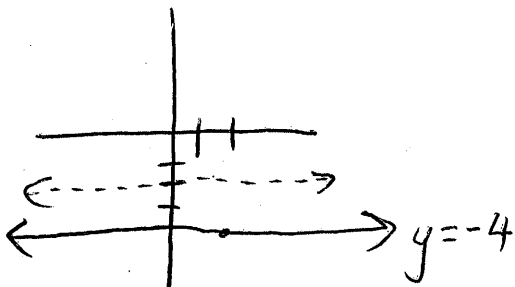
$$y - 1 = -\frac{4}{5}(x + 5)$$

- 9) Write an equation of the line that passes through $(-3, 7)$ and is perpendicular to the line $x = 1$



$$y = 7$$

- 10) Write an equation of the line that passes through $(2, -4)$ and is parallel to the line $y = -2$



$$y = -4$$