

Name: _____
 Period: _____

Date: _____

Key

5

Essential Question: What are the similarities and differences between the special quadrilaterals?

Each of these shapes is a parallelogram, so they each have the properties of parallelograms (listed below), plus more of their own.

Theorems about Rhombuses (use Rhombus EFGH below to fill in the blanks):

1. A parallelogram is a rhombus if and only if its diagonals are perpendicular.

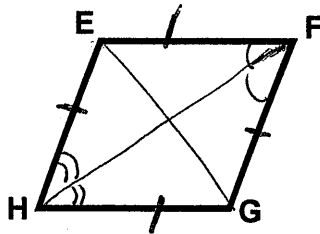
$$\underline{HF \perp EG}$$

2. A parallelogram is a rhombus if and only if each diagonal bisects a pair of opposite angles.

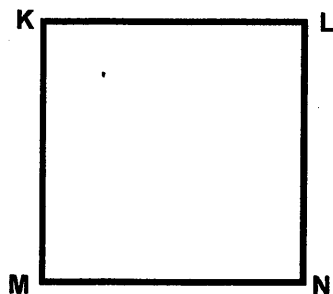
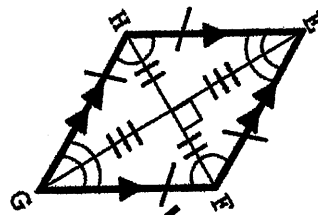
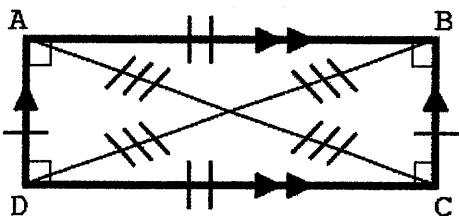
$$\underline{EG} \text{ bisects } \angle HEF \text{ and } \angle HGF, \text{ so } \underline{\angle HEG \cong \angle FEG} \text{ and } \underline{\angle HGE \cong \angle FGE}$$

$$\underline{FH} \text{ bisects } \angle EFG \text{ and } \angle EHG, \text{ so } \underline{\angle EHF \cong \angle FHG} \text{ and } \underline{\angle EFH \cong \angle GFH}$$

3. All four sides are equal.



There are no theorems specific to the square. It is special because it has all of the properties of the rectangle and rhombus.



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Example 1: Decide whether the statement is *always*, *sometimes*, or *never* true.

a. A rectangle is a square.

sometimes never

b. A square is a parallelogram.

always

c. A quadrilateral is a rhombus.

sometimes

d. A square is a rectangle.

always

Example 2: Solve for x using the figure to the right.

a. $m\angle RBH = 8x - 6$

$$8x - 6 = 90$$

$$x = 12$$

$$8x = 96$$

b. $m\angle RHM = x + 40$ and $m\angle MRH = 2x$

$$2x + 80 + 2x = 180$$

$$4x + 80 = 180$$

$$4x = 100$$

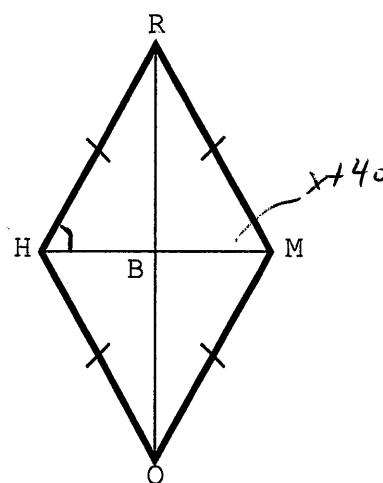
$$x = 25$$

c. If $m\angle HOB = 24^\circ$, find $m\angle MOB$.

$$24^\circ$$

d. If $RB = 6$, find RO .

$$12$$



Example 3: WXYZ is a square. If WT is 3, find each measure.

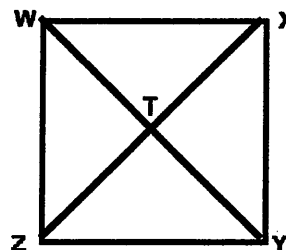
a. ZX 6

b. WX $3\sqrt{2}$

c. $\angle WZY$ 90°

d. $\angle XYT$ 45°

e. $\angle ZTY$ 90°



6-5 Practice

Rhombi and Squares

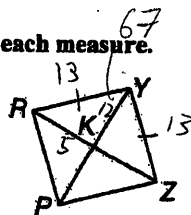
$PRYZ$ is a rhombus. If $RK = 5$, $RY = 13$ and $m\angle YRZ = 67$, find each measure.

1. KY 12

2. PK 5

3. $m\angle YKZ$ 90°

4. $m\angle PZR$ 45°



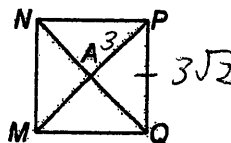
$MNPQ$ is a rhombus. If $PQ = 3\sqrt{2}$ and $AP = 3$, find each measure.

5. AQ 3

6. $m\angle APQ$ 45°

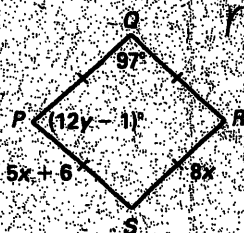
7. $m\angle MNP$ 90°

8. PM $3\sqrt{2}$



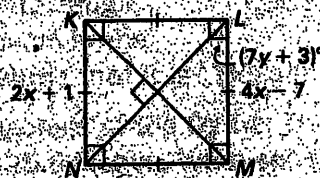
Classify the special quadrilateral. Explain your reasoning. Then find the values of x and y .

11.



rhombus

12.



square

$$8x = 5x + 6$$

$$3x = 6$$

$$x = 2$$

$$12y - 1 + 97 = 180$$

$$12y + 96 = 180$$

$$4x - 7 = 2x + 1$$

$$2x = 8$$

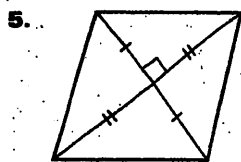
$$x = 4$$

$$7y + 3 = 45$$

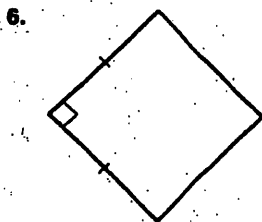
$$7y = 42$$

$$y = 6$$

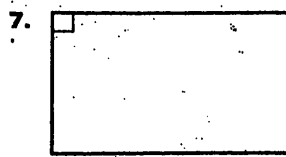
Classify the parallelogram. Explain your reasoning.



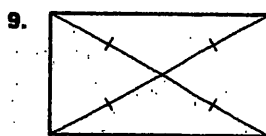
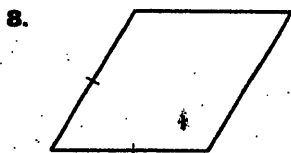
rhombus



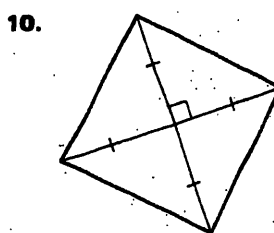
square



rectangle



rectangle



$$\begin{array}{r}
 15 \\
 \hline
 4 \\
 \hline
 -7 \\
 \hline
 \end{array}
 \begin{array}{r}
 3 \\
 \hline
 -3 \\
 \hline
 -9 \\
 \hline
 \end{array}$$

Handwritten notes: +11, 11, 6, 6

Key

Quadrilaterals Quiz Review #2

Date

Period

Find the midpoint of the line segment with the given endpoints.

1) $(-7, 9), (8, -6)$

$\left(\frac{1}{2}, 1\frac{1}{2}\right)$

$\frac{-7+8}{2}, \frac{9-6}{2}$

$M\left(\frac{1}{2}, \frac{3}{2}\right)$

Find the other endpoint of the line segment with the given endpoint and midpoint.

2) Endpoint: $(-7, -9)$, midpoint: $(4, -3)$

$(15, 3)$

$+11 \begin{bmatrix} 15 & 3 \\ 4 & -3 \end{bmatrix} + 6$
 $M \begin{bmatrix} 4 & -3 \\ -7 & -9 \end{bmatrix} + 6$

$E(15, 3)$

Find the distance between each pair of points. Round your answer to the nearest tenth, if necessary.

3) $(7.4, -1.9), (-7.9, -3.4)$

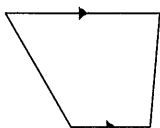
15.4

$d^2 = (-7.9 - 7.4)^2 + (-3.4 - (-1.9))^2$

$d = 15.4$

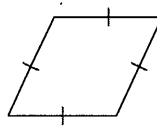
State the most specific name for each figure.

4)



trapezoid

5)



rhombus

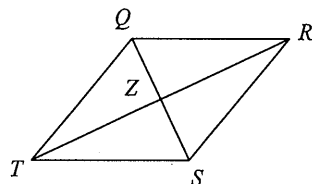
Solve for x . Each figure is a parallelogram.

6) $ZT = 21$

$RT = 7x - 7$

$2(21) = 7x - 7$

7

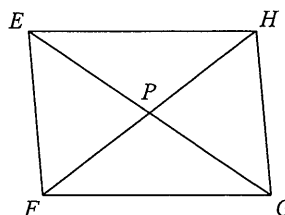


7) $GP = 1 + 3x$

$PE = 4x - 1$

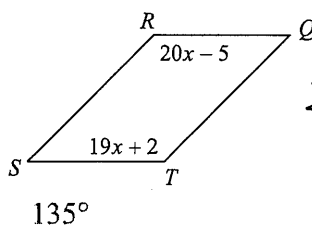
$4x - 1 = 1 + 3x$

2



Find the measurement indicated in each parallelogram.

8) Find $m\angle R$

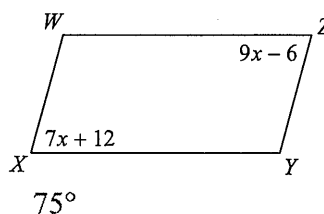


$20x - 5 = 19x + 2$

$1x = 7$

$m\angle R = 20(7) - 5$

9) Find $m\angle X$



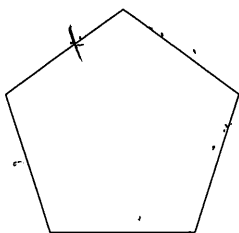
$9x - 6 = 7x + 12$

$2x = 18$

$x = 9$

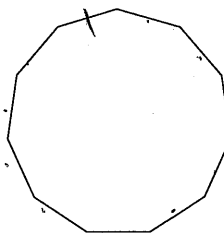
Find the measure of one interior angle in each polygon. Round your answer to the nearest tenth if necessary.

10) $n=5$ $\text{Angle} = \frac{180(5-2)}{5}$



108°

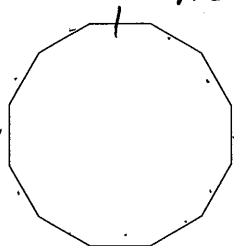
11) $n=11$



147.3°

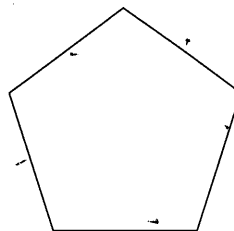
Find the measure of one exterior angle in each polygon. Round your answer to the nearest tenth if necessary.

12) $n=12$



30°

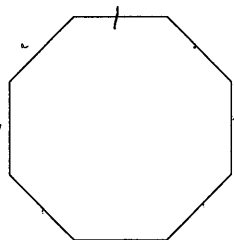
13) $n=5$



72°

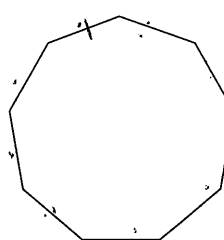
Find the interior angle sum for each polygon. Round your answer to the nearest tenth if necessary.

14) $n=8$



1080°

15) $n=9$



1260°