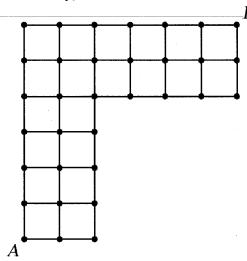
## **Math Team State Tournament 2015 Problems**

The street map below shows the only routes in a rectangular coordinate system. Using this map, how many different shortest paths, along streets only, are there from A to B?



- (A) 100
- **(B)** 262
- **(C)** 297
- **(D)** 924
- **(E)** 927

Heron's formula states that the area of a triangle whose sides have lengths a, b, and c is

$$A = \sqrt{s(s-a)(s-b)(s-c)},$$

where s is the semiperimeter of the triangle; that is,

$$s = \frac{a+b+c}{2}.$$

- Compute the area of a triangle whose side lengths are 9, 11, and 14.
  - (A)  $11\sqrt{17}$
- **(B)**  $12\sqrt{17}$  **(C)**  $11\sqrt{34}$
- **(D)** 77
- **(E)** 99

3) Let N be the base-3 number 221221. When N is written in base-9, what is its left-most digit?

(A) 1 (B) 2 (C) 6 (D) 7 (E) 8

- 4) Evaluate  $\frac{1}{20 + \frac{1}{15 + \frac{1}{20 + \frac{1}{15 + \cdots}}}}$  to the nearest thousandth.
  - (A) 0.047 (B) 0.048 (C) 0.049 (D) 0.050 (E) 0.051

Given  $\log_2(\log_2(\log_3 x)) = \log_2(\log_3(\log_2 y)) = 0$ , compute the value of x - y.

(A) -1 (B) 0 (C) 1 (D) 2 (E) 17