

Determining Types of Convergence Tests:

1) Always **Start with nth term test** unless the series is instantly recognizable
(geometric series or p-series)

2) Does it look like a Geometric Series? $\sum_{n=0}^{\infty} \left(\frac{2}{7}\right)^n$ Or $\sum_{n=1}^{\infty} \frac{7^{n-2}}{8^{n+1}}$
(Know how to find Sum of Geometric Series!)

3) Does it look like a P-Series Test? $\sum_{n=1}^{\infty} \frac{4}{n^3}$

4) Does it look like Integral Test? $\sum_{n=2}^{\infty} \frac{1}{n(\ln n)^4}$
(does it look like a u-substitution problem?)

(Remember conditions for Integral Test: positive, decreasing, continuous)

5) Does it look a good fit for Limit Comparison Test? $\sum_{n=1}^{\infty} \frac{5n^2 - 6n + 3}{n^3 - 7n + 8}$

6) Does it look like an Alternating Series? $\sum_{n=1}^{\infty} \frac{(-1)^n}{\ln n}$

7) Does it look like a good fit for Ratio Test? $\sum_{n=1}^{\infty} \frac{n!}{10^n}$ or $\sum_{n=1}^{\infty} \frac{3^{n-1}}{n2^n}$
(factorials and/or exponentials involved)

8) Does it look like a Root Test problem?
(entire expression is raised to the nth power) $\sum_{n=1}^{\infty} \left(\frac{n+1}{2n+1}\right)^n$

9) Direct Comparison can be an option when LCT
doesn't quite seem to be a good fit $\sum_{n=1}^{\infty} \frac{1}{n + n \cos^2(n)}$

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$$\sum_{n=2}^{\infty} \frac{1}{n(\ln n)^4} \rightarrow \int \frac{1}{x(\ln x)^4} dx$$

$$\sum \frac{5n^3 - 6n}{4n^2 + 8n}$$

5) Does it look a good fit for Limit Comparison Test?

$$\sum_{n=1}^{\infty} \frac{5n^2 - 6n + 3}{n^3 - 7n + 8}$$

↑
nth term test

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$$\sum_{n=1}^{\infty} \frac{1}{n + n \cos^2(n)}$$

DCT Compare with $\frac{1}{2n}$

$$\left[\text{Diverges by DCT} \right] \quad \frac{1}{2n} \leq \frac{1}{n + n \cos^2 n}$$