

Volumes of Prisms and Pyramids

Key

Prism: a solid having bases or ends that are parallel, congruent polygons and sides that are parallelograms.

A solid object with two identical ends and flat sides:

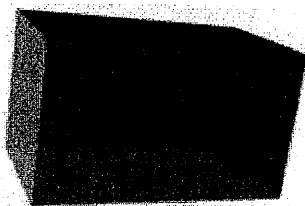
- The sides are parallelograms (4-sided shape with opposite sides parallel)
- The cross section is the same all along its length

Cross section is the shape made when a solid is cut through parallel to the base.

The shape of the ends give the prism a name, such as "triangular prism"

These are all Prisms:

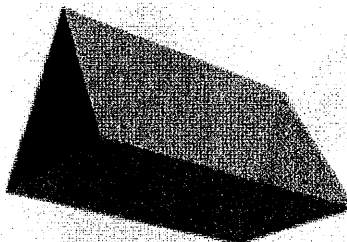
Square Prism:



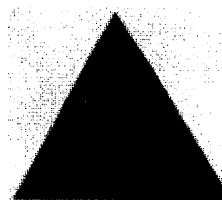
Cross-Section:



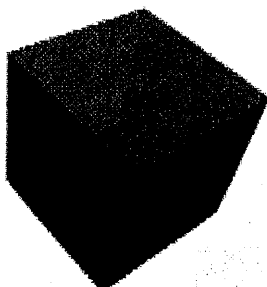
Triangular Prism:



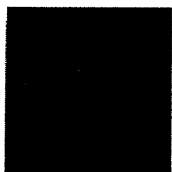
Cross-Section:



Cube:



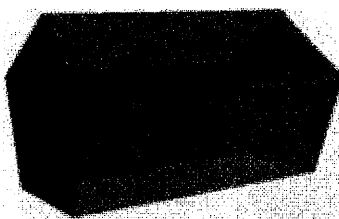
Cross-Section:



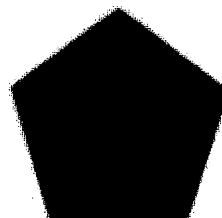
(yes, a cube is a prism, because it is a square all along its length)

(Also see Rectangular Prisms)

Pentagonal Prism:

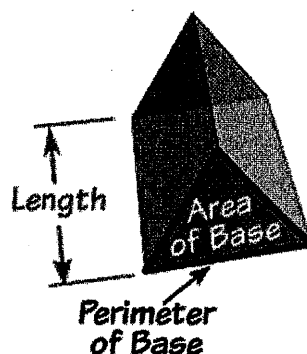


Cross-Section:

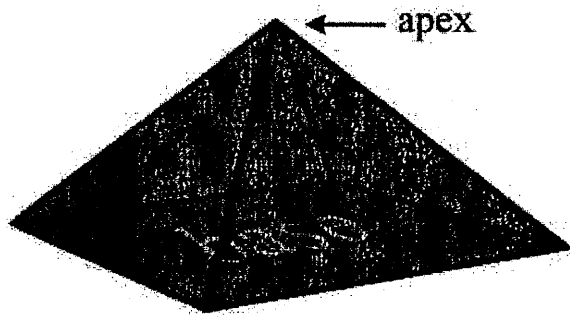


The Volume of a prism is the area of one end times the length of the prism.

$$\text{Volume} = \text{Base Area} \times \text{Length}$$

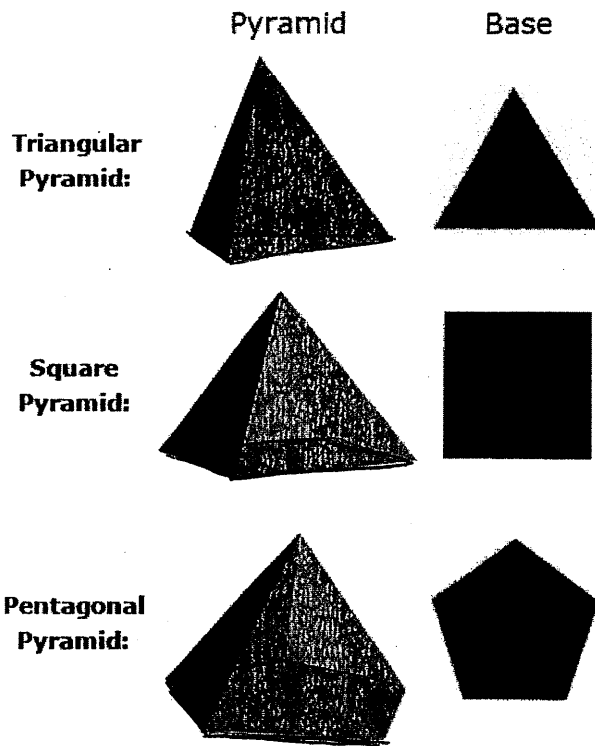


Pyramids: a shape or structure with a polygon for its base and three or more triangles for its sides which meet to form the top.



A solid object where:

- The base is a polygon (a straight-sided flat shape)
- The sides are triangles which meet at the top (the apex).



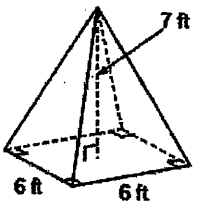
The Volume of a Pyramid

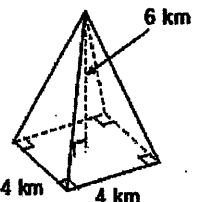
- $\frac{1}{3} \times [\text{Base Area}] \times \text{Height}$

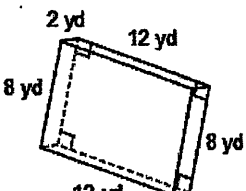
12-4 and 12-5 Volume of Prisms and Pyramids

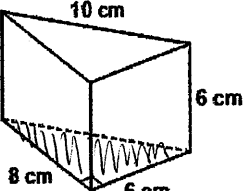
Key

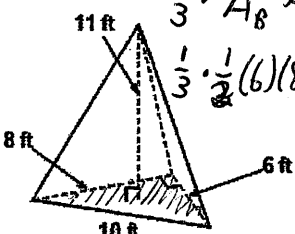
Find the volume of each figure. Round your answers to the nearest hundredth, if necessary.

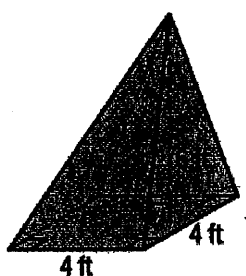
1)  $\frac{1}{3} \cdot 6^2 \cdot 7$
 84 ft^3

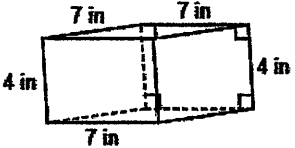
2)  $\frac{1}{3} \cdot 16 \cdot 6 =$
 32 km^3

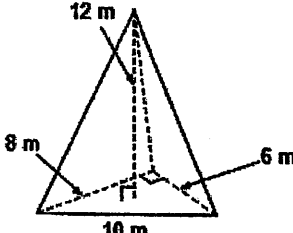
3) $V = A_B \times h$
 $= 2 \cdot 8 \cdot 12$
 $= 192 \text{ yd}^3$

4)  $\frac{1}{2}(6)(8) \times 6$
 $V = 144 \text{ cm}^3$

5) $\frac{1}{3} \times A_B \times h$
 $\frac{1}{3} \cdot \frac{1}{2}(6)(8) \times 11$
 88 ft^3

6)  $\frac{1}{3} A_B \times h$
 $\frac{1}{3}(4)^2 \times 6$
 32 ft^3

7)  $7^2 \times 4 =$
 196 in^3

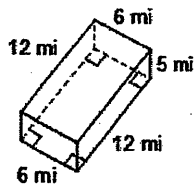
8) 

$$V = \frac{1}{3} \times A_T \times h$$

$$V = \frac{1}{3} \times \frac{1}{2}(6)(8) \times 12$$

$$V = 96 \text{ m}^3$$

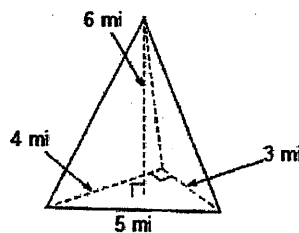
9)



$$5 \times 6 \times 12$$

$$360 \text{ mi}^3$$

10)

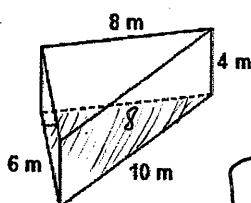


$$\frac{1}{3} \times A_T \times h$$

$$\frac{1}{3} \times \frac{1}{2}(3)(4) \times 6$$

$$12 \text{ mi}^3$$

11)

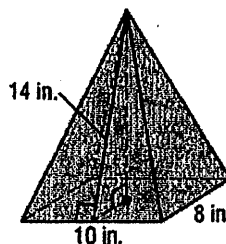


$$V = A_T \times h$$

$$V = \frac{1}{2}(6)(8) \times 4$$

$$V = 48 \text{ m}^3$$

12)

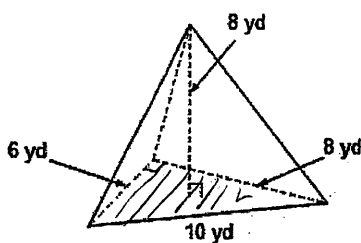


$$V = \frac{1}{3} \times A_T \times h$$

$$V = \frac{1}{3} \times (8)(10) \times 14$$

$$V = \frac{1120}{3} \text{ in}^3$$

13)

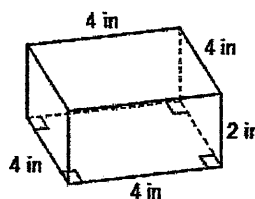


$$V = \frac{1}{3} \times A_T \times h$$

$$V = \frac{1}{3} \times \frac{1}{2}(6)(8) \times 8$$

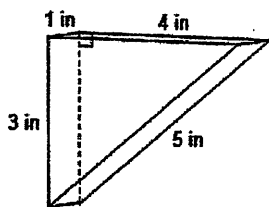
$$= 64 \text{ yd}^3$$

14)



$$V = 4^2 \times 2 = 32 \text{ in}^3$$

15)



$$V = A_T \times h$$

$$= \frac{1}{2}(3)(4) \times 1$$

$$V = 6 \text{ in}^3$$