

~~11/7/2014~~

KEY

Tues 11/11/14

6.7 Circumference & Arc Length

Page 218 – 229

2)

Circumference

- Defn. – the distance around a circle.
 - Theorem– Circumference of a Circle –
$$C = 2\pi r \quad \text{or} \quad C = \pi d$$
- * Always use the π button on your calculator,
NOT 3.14!!!

3)

Ex: Find the circumference of a circle with a diameter of 12 cm.
 (Round to 2 decimal places.)

$$r = 6$$

$$C = 2\pi r$$

$$C = 2\pi(6)$$

$$C = 12\pi \text{ cm}$$

4)

Ex: Find the radius of a circle with a circumference of 52 in.

$$C = 52$$

$$C = 2\pi r$$

$$52 = 2\pi r$$

$$\frac{52}{2\pi} = r$$

$$\frac{26}{\pi} = r$$

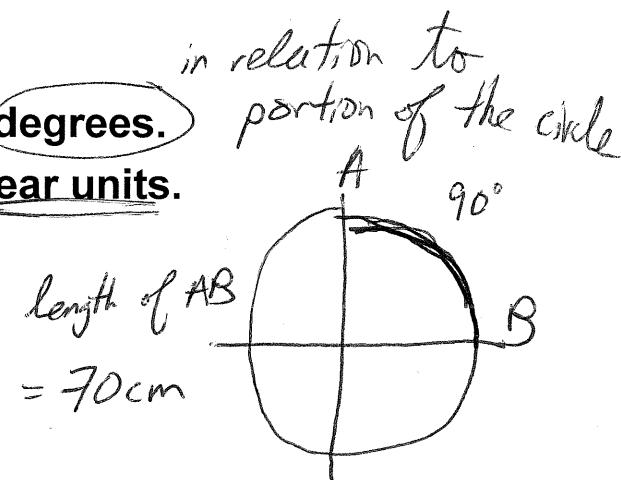
$$r = \frac{26}{\pi} \text{ in.} \quad \approx 8.28$$

5)

Arc Length

- **Definition.** – a piece of the circumference of a circle.

- The measure of an arc is in **degrees**.
- The length of an arc is in linear units.
(such as ft, cm, etc.)



6)

Arc Length Corollary

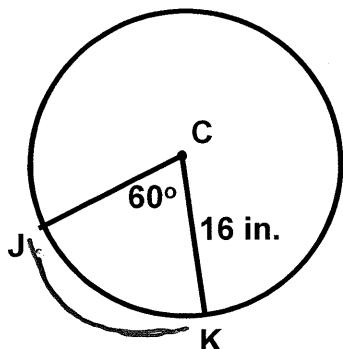
- The length of \widehat{AB} is:

fraction of circle $\left\{ \frac{m \widehat{AB}}{360^\circ} * 2\pi r \right\}$

7)

Ex: Find the length of \widehat{JK} .

$$\frac{m \widehat{JK}}{360^\circ} * 2\pi r$$



$$\frac{60}{360} * 2\pi(16)$$

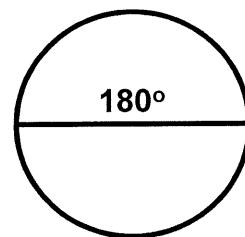
$$\frac{1}{6} * 32\pi = \boxed{\frac{16\pi}{3} \text{ in.}}$$

$$\boxed{16.76 \text{ in.}}$$

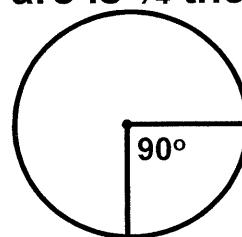
8)

Arc Length Corollary Observations

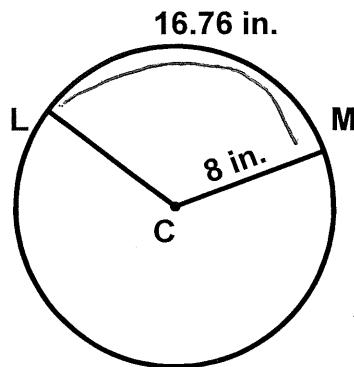
- The length of a semicircle is $\frac{1}{2}$ the circumference.



- The length of a 90° arc is $\frac{1}{4}$ the circumference.



9)

Ex: Find the $m \widehat{LM}$.

$$\frac{16.76}{2\pi r} = \frac{\text{Arc}}{360}$$

$$\text{length of } \widehat{LM} = \frac{m \widehat{LM}}{360^\circ} * 2\pi r$$

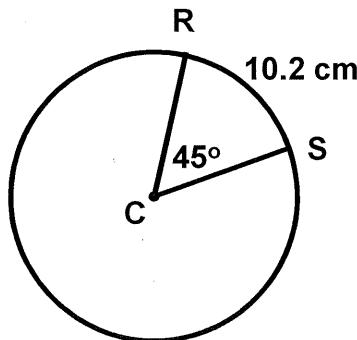
$$L = \frac{m \widehat{LM}}{360} * 2\pi r$$

$$\frac{16.76}{2\pi(8)} = \frac{\text{Arc}}{360}$$

$$\frac{(360)(16.76)}{16\pi} = \frac{\text{Arc}(16\pi)}{16\pi}$$

$$\text{Arc} = 120.03^\circ$$

10)

Ex: Find the circumference of circle C.

$$\text{length of } \widehat{RS} = \frac{m \widehat{RS}}{360^\circ} * 2\pi r$$

$$\frac{\text{Length}}{2\pi r} = \frac{\text{Arc}}{360^\circ}$$

* Find radius first

$$\frac{10.2}{2\pi r} = \frac{45}{360}$$

$$\frac{10.2}{2\pi r} = \frac{1}{8}$$

$$\frac{10.2(8)}{2\pi} = r$$

$$(10.2)(8) = 2\pi r$$

$$12.98 = r$$

$$C = 2\pi r$$

$$C = 2\pi(12.98)$$

$$C = 81.6 \text{ cm}$$

Assignment
Page 228 – 229
#s 1 – 21 all