

Steps for Solving by Completing the Square method

1. Arrange terms in standard form :  $ax^2 + bx + c = 0$
2. "a" value MUST be equal to 1, so divide each term by the GCF to make  $a = 1$
3. Move constant to the other side of the equation and add spaces to each side

$$\boxed{x^2 + bx + \underline{\quad} = c + \underline{\quad}}$$

4. Find  $\left(\frac{b}{2}\right)^2$  and enter this value into the blank spaces  $\underline{\quad}$  on both sides of the equation
5. Rewrite left side in factored form and add the numbers on the right side
6. take the  $\sqrt{\quad}$  of both sides (don't forget  $\pm$ )
7. solve for x

Solve the quadratic equations below using complete the square method:

1.  $x^2 - 8x - 16 = 3$

2.  $4x^2 - 16x - 27 = 1$

3.  $2x^2 - 8x = 32$

4.  $5x^2 - 30x - 5$

1. Arrange terms in standard form :  $ax^2 + bx + c = 0$
2. "a" value MUST be equal to 1, so divide each term by the GCF to make  $a = 1$
3. Move constant to the other side of the equation and add spaces to each side

$$\boxed{x^2 + bx + \underline{\quad} = c + \underline{\quad}}$$

4. Find  $\left(\frac{b}{2}\right)^2$  and enter this value into the blank spaces  $\underline{\quad}$  on both sides of the equation

5. Rewrite left side in factored form and add the numbers on the right side

6. take the  $\sqrt{\quad}$  of both sides (don't forget  $\pm$ )

7. solve for x

5.  $4x^2 - 24x - 3 = 1$

6.  $6x^2 - 12x - 41 = 1$

7.  $x^2 - 4x - 12 = 2$

8.  $3x^2 - 36x - 7 = -1$

# Complete the Square Practice

Monday Sept 21, 2015

Key

Steps for Solving by Completing the Square method

1. Arrange terms in standard form :  $ax^2 + bx + c = 0$
2. "a" value MUST be equal to 1, so divide each term by the GCF to make  $a = 1$
3. Move constant to the other side of the equation and add spaces to each side

$$\boxed{x^2 + bx + \underline{\quad} = c + \underline{\quad}}$$

4. Find  $\left(\frac{b}{2}\right)^2$  and enter this value into the blank spaces  $\underline{\quad}$  on both sides of the equation
5. Rewrite left side in factored form and add the numbers on the right side
6. take the  $\sqrt{\quad}$  of both sides (don't forget  $\pm$ )
7. solve for x

Solve the quadratic equations below using complete the square method:

1.  $x^2 - 8x - 16 = 3$        $x^2 - 8x - 19 = 0$

$$x^2 - 8x + 16 = 19 + 16 \quad \left(\frac{8}{2}\right)^2 = 4^2 = 16$$

$$(x - 4)^2 = 35$$

$$\sqrt{(x - 4)^2} = \pm\sqrt{35}$$

$$x - 4 = \pm\sqrt{35}$$

$$\boxed{x = 4 \pm \sqrt{35}}$$

2.  $4x^2 - 16x - 27 = 1$

$$\frac{4x^2}{4} - \frac{16x}{4} - \frac{28}{4} = 0$$

$$x^2 - 4x - 7 = 0$$

$$x^2 - 4x + 4 = 7 + 4$$

$$\left(\frac{b}{2}\right)^2 = \left(\frac{-4}{2}\right)^2 = 4$$

$$\sqrt{(x - 2)^2} = \pm\sqrt{11}$$

$$x - 2 = \pm\sqrt{11}$$

$$\boxed{x = 2 \pm \sqrt{11}}$$

3.  $2x^2 - 8x = 32$

$$\frac{2x^2}{2} - \frac{8x}{2} - \frac{32}{2} = 0$$

$$x^2 - 4x - 16 = 0 \quad \left(\frac{-4}{2}\right)^2 = 4$$

$$x^2 - 4x + 4 = 16 + 4$$

$$\sqrt{(x - 2)^2} = \pm\sqrt{20}$$

$$x - 2 = \pm\sqrt{20}$$

$$\boxed{x = 2 \pm \sqrt{20}} \quad \boxed{2 \pm 2\sqrt{5}}$$

4.  $5x^2 - 30x - 5 = 0$

$$\left(\frac{b}{2}\right)^2 = \left(\frac{-6}{2}\right)^2 = 9$$

$$x^2 - 6x - 1 = 0$$

$$x^2 - 6x + 9 = 1 + 9$$

$$\sqrt{(x - 3)^2} = \pm\sqrt{10}$$

$$x - 3 = \pm\sqrt{10}$$

$$x = 3 \pm \sqrt{10}$$

1. Arrange terms in standard form:  $ax^2 + bx + c = 0$
2. "a" value MUST be equal to 1, so divide each term by the GCF to make  $a = 1$
3. Move constant to the other side of the equation and add spaces to each side

$$\boxed{x^2 + bx + \underline{\quad} = c + \underline{\quad}}$$

4. Find  $\left(\frac{b}{2}\right)^2$  and enter this value into the blank spaces  $\underline{\quad}$  on both sides of the equation

5. Rewrite left side in factored form and add the numbers on the right side

6. take the  $\sqrt{\quad}$  of both sides (don't forget  $\pm$ )

7. solve for x

3.  $4x^2 - 24x - 3 = 1$

5)  $\frac{4x^2}{4} - \frac{24x}{4} - \frac{4}{4} = \frac{0}{4}$

$$x^2 - 6x - 1 = 0 \quad \left(\frac{6}{2}\right)^2 = \left(\frac{6}{2}\right)^2 = 9$$

$$x^2 - 6x + \underline{9} = 1 + \underline{9}$$

$$\sqrt{(x-3)^2} = \pm\sqrt{10}$$

$$x-3 = \pm\sqrt{10}$$

$$\boxed{x = 3 \pm \sqrt{10}}$$

4.  $6x^2 - 12x - 41 = 1$

6)  $\frac{6x^2}{6} - \frac{12x}{6} - \frac{42}{6} = \frac{0}{6}$

$$x^2 - 2x - 7 = 0 \quad \left(\frac{2}{2}\right)^2 = \left(\frac{-2}{2}\right)^2 = 1$$

$$x^2 - 2x + \underline{1} = 7 + \underline{1}$$

$$\sqrt{(x-1)^2} = \pm\sqrt{8}$$

$$x-1 = \pm\sqrt{8}$$

$$\boxed{x = 1 \pm \sqrt{8} \text{ or } x = 1 \pm 2\sqrt{2}}$$

7) 5.  $x^2 - 4x - 12 = 2$

$$x^2 - 4x - 14 = 0$$

$$x^2 - 4x + \underline{4} = 14 + \underline{4}$$

$$\sqrt{(x-2)^2} = \pm\sqrt{18}$$

$$x-2 = \pm\sqrt{18}$$

$$x = 2 \pm \sqrt{18}$$

or

$$\boxed{x = 2 \pm 3\sqrt{2}}$$

$$\left(\frac{4}{2}\right)^2 = \left(\frac{4}{2}\right)^2 = 4$$

8) 6.  $3x^2 - 36x - 7 = -1$

$$\frac{3x^2}{3} - \frac{36x}{3} - \frac{6}{3} = \frac{0}{3}$$

$$x^2 - 12x - 2 = 0$$

$$x^2 - 12x + \underline{36} = 2 + \underline{36}$$

$$\sqrt{(x-6)^2} = \pm\sqrt{38}$$

$$x-6 = \pm\sqrt{38}$$

$$\boxed{x = 6 \pm \sqrt{38}}$$

$$\left(\frac{12}{2}\right)^2 = 6^2 = 36$$