

AP Calculus AB Derivative & Integral Rules Formula Patterns

I. Derivative Rules

A. Trig Derivatives

$$1) \frac{d}{dx} \sin u = \cos u * u'$$

$$2) \frac{d}{dx} \cos u = -\sin u * u'$$

$$3) \frac{d}{dx} \tan u = \sec^2 u * u'$$

$$4) \frac{d}{dx} \cot u = -\csc^2 u * u'$$

$$5) \frac{d}{dx} \sec u = \sec u \tan u * u'$$

$$6) \frac{d}{dx} \csc u = -\csc u \cot u * u'$$

B. Logs and Exponential Derivatives

$$7) \frac{d}{dx} \ln u = \frac{u'}{u}$$

$$8) \frac{d}{dx} e^u = e^u * u'$$

$$9) \frac{d}{dx} \log_a u = \left(\frac{1}{\ln a}\right) \frac{u'}{u}$$

$$10) \frac{d}{dx} a^u = (\ln a) a^u * u'$$

C. ArcTrig Derivatives

$$11) \frac{d}{dx} \arcsin u = \frac{u'}{\sqrt{1-u^2}}$$

$$12) \frac{d}{dx} \arccos u = -\frac{u'}{\sqrt{1-u^2}}$$

$$13) \frac{d}{dx} \arctan u = \frac{u'}{1+u^2}$$

$$14) \frac{d}{dx} \text{arccot } u = -\frac{u'}{1+u^2}$$

$$15) \frac{d}{dx} \text{arcsec } u = \frac{u'}{|u|\sqrt{u^2-1}}$$

$$16) \frac{d}{dx} \text{arccsc } u = -\frac{u'}{|u|\sqrt{u^2-1}}$$

II. Integral Rules

A. Basic Trig Integrals

1) $\int \sin u \, du = -\cos u + C$

2) $\int \cos u \, du = \sin u + C$

3) $\int \sec^2 u \, du = \tan u + C$

4) $\int \sec u \tan u \, du = \sec u + C$

5) $\int \csc^2 u \, du = -\cot u + C$

6) $\int \csc u \cot u \, du = -\csc u + C$

B. Trig Integrals involving Natural Logs

7) $\int \tan u \, du = -\ln|\cos u| + C$

8) $\int \cot u \, du = \ln|\sin u| + C$

9) $\int \sec u \, du = \ln|\sec u + \tan u| + C$

10) $\int \csc u \, du = -\ln|\csc u + \cot u| + C$

C. Power Rule, Logs and Exponentials

11) $\int u^n \, du = \frac{u^{n+1}}{n+1} + C$

12) $\int \frac{1}{u} \, du = \ln|u| + C$

13) $\int e^u \, du = e^u + C$

14) $\int a^u \, du = \left(\frac{1}{\ln a}\right) a^u + C$

D. Inverse Trig Integrals

15) $\int \frac{1}{\sqrt{a^2-u^2}} \, du = \arcsin\left(\frac{u}{a}\right) + C$

16) $\int \frac{1}{a^2+u^2} \, du = \frac{1}{a} \arctan\left(\frac{u}{a}\right) + C$

17) $\int \frac{1}{u\sqrt{u^2-a^2}} \, du = \frac{1}{a} \operatorname{arcsec}\left(\frac{|u|}{a}\right) + C$

AP Calculus AB Derivative & Integral Rules Formula Patterns (Blank Practice Sheet)

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