

Key

Solve by Factoring #1-6

1. $7x^2 = 6 - 19x$

$\frac{-2}{-2} \times \frac{21}{+21} = -42$
 $\frac{-2}{-2} + \frac{21}{+21} = 19$

$7x^2 + 19x - 6 = 0$

$\sqrt{\frac{7x^2}{x} - \frac{2x}{x} + \frac{21x}{3} - \frac{6}{3}} = 0$

$x(7x - 2) + 3(7x - 2) = 0$

$(7x - 2)(x + 3)$

$x = \frac{2}{7} \quad x = -3$

2. $15x^2 = 65x - 20$

$\frac{-1}{-1} \times \frac{12}{+12} = 12$
 $\frac{-1}{-1} + \frac{12}{+12} = -13$

$\frac{15x^2}{5} - \frac{65x}{5} + \frac{20}{5} = 0$

$5(3x^2 - 13x + 4)$

$\sqrt{\frac{3x^2}{x} - \frac{1x}{x} - \frac{12x}{-4} + \frac{4}{-4}}$

$x(3x - 1) - 4(3x - 1)$

$5(x - 4)(3x - 1)$

$x = 4, \frac{1}{3}$

3. $8x^2 = 18$

$\frac{8x^2}{2} - \frac{18}{2} = 0$

$2(4x^2 - 9) = 0$

$\frac{6}{6} \times \frac{-6}{-6} = -36$
 $\frac{6}{6} + \frac{-6}{-6} = 0$

$4x^2 + 0x - 9 = 0$

$\sqrt{\frac{4x^2}{2x} + \frac{6x}{2x} - \frac{6x}{-3} - \frac{9}{-3}} = 0$

$2x(2x + 3) - 3(2x + 3)$

$2(2x + 3)(2x - 3)$

$x = -\frac{3}{2}, \frac{3}{2}$

4. $12x^2 = 30x$

$\frac{12x^2}{6x} - \frac{30x}{6x} = 0$

$6x(2x - 5)$

$x = 0, x = \frac{5}{2}$

5. $12x^2 - 10 = -26x$

$\frac{15}{15} \times \frac{-2}{+2} = -30$
 $\frac{15}{15} + \frac{-2}{+2} = 13$

$\frac{12x^2}{2} + \frac{26x}{2} - \frac{10}{2} = 0$

$2(6x^2 + 13x - 5) = 0$

$\sqrt{\frac{6x^2}{3x} + \frac{15x}{3x} - \frac{2x}{-1} - \frac{5}{-1}}$

$3x(2x + 5) - 1(2x + 5)$

$(2x + 5)(3x - 1)$

$x = -\frac{5}{2}, x = \frac{1}{3}$

6. $9x^2 - 9 = 72$

$\frac{9x^2}{9} - \frac{81}{9} = 0$

$9x^2 - 9 - 72 = 0$

$9(x^2 - 9) = 0$

$\frac{3}{3} \times \frac{-3}{-3} = -9$
 $\frac{3}{3} + \frac{-3}{-3} = 0$

$9(x^2 + 0x - 9) = 0$

$\sqrt{\frac{x^2}{x} + \frac{3x}{x} - \frac{3x}{-3} - \frac{9}{-3}}$

$x(x + 3) - 3(x + 3)$

$(x + 3)(x - 3)$

$x = -3, x = 3$

For #7 - 10, solve by completing the square

7. $6x^2 = 10x + 2x + 63 + 3$

$$\frac{6x^2}{6} - \frac{12x}{6} - \frac{66}{6} = \frac{0}{6} \quad \left| \left(\frac{b}{2}\right)^2 = \left(\frac{-2}{2}\right)^2 = 1 \right.$$

$$x^2 - 2x - 11 = 0$$

$$x^2 - 2x + \underline{1} = 11 + \underline{1}$$

$$(x - 1)^2 = 12$$

$$\sqrt{(x-1)^2} = \pm\sqrt{12}$$

$$x - 1 = \pm\sqrt{12}$$

$$x = 1 \pm \sqrt{12}$$

or

$$x = 1 \pm 2\sqrt{3}$$

8. $6x^2 - 12x - 41 = 1$

$$\frac{6x^2}{6} - \frac{12x}{6} - \frac{42}{6} = \frac{0}{6} \quad \left| \left(\frac{b}{2}\right)^2 = \left(\frac{-2}{2}\right)^2 = 1 \right.$$

$$x^2 - 2x - 7 = 0$$

$$x^2 - 2x + \underline{1} = 7 + \underline{1}$$

$$(x - 1)^2 = 8$$

$$\sqrt{(x-1)^2} = \pm\sqrt{8}$$

$$x - 1 = \pm\sqrt{8}$$

$$x - 1 = \pm\sqrt{8}$$

$$x = 1 \pm \sqrt{8}$$

or

$$x = 1 \pm 2\sqrt{2}$$

9. $x^2 - 13 = 12x - 1$

$$x^2 - 12x - 12 = 0$$

$$\left(\frac{b}{2}\right)^2 = \left(\frac{12}{2}\right)^2 = 6^2 = 36$$

$$x^2 - 12x + \underline{36} = 12 + \underline{36}$$

$$(x - 6)^2 = 48$$

$$\sqrt{(x-6)^2} = \pm\sqrt{48}$$

$$x - 6 = \pm\sqrt{48}$$

$$x = 6 \pm \sqrt{48}$$

or

$$x = 6 \pm 4\sqrt{3}$$

10. $2x^2 = 16x + 26$

$$\frac{2x^2}{2} - \frac{16x}{2} - \frac{26}{2} = \frac{0}{2}$$

$$\left(\frac{b}{2}\right)^2 = \left(\frac{-8}{2}\right)^2 = 4^2 = 16$$

$$x^2 - 8x - 13 = 0$$

$$x^2 - 8x + \underline{16} = 13 + \underline{16}$$

$$(x - 4)^2 = 29$$

$$\sqrt{(x-4)^2} = \pm\sqrt{29}$$

$$x - 4 = \pm\sqrt{29}$$

Use quadratic equation and discriminant to solve: Quadratic Equation: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

11. Use quadratic formula to solve: $4x^2 = 1x - 6$

$$4x^2 - 1x + 6 = 0$$

$$a = 4$$

$$b = -1$$

$$D = 1^2 - (4 \cdot 4 \cdot 6) = -95 \quad c = 6$$

$$x = \frac{1 \pm \sqrt{-95}}{2(4)} = \frac{1 \pm \sqrt{-95}}{8}$$

Discriminant -95

Nature of solution: No Real
(2 imaginary solutions)

Solution(s) $\frac{1 \pm \sqrt{-95}}{8}$

12. Use quadratic formula to solve: $3x^2 + 1 - x = 5x + 9$

$$a = 3$$

$$b = -6$$

$$c = -8$$

$$3x^2 - 6x - 8 = 0$$

$$D = 6^2 - (4 \cdot 3 \cdot -8) = 132$$

$$x = \frac{6 \pm \sqrt{132}}{2(3)} = \frac{6 \pm \sqrt{132}}{6}$$

Discriminant 132

Nature of solution: 2 Real

Solution(s) $\frac{6 \pm \sqrt{132}}{6}$