

CCGPS Analytic Geometry Probability Test Review I

1. Your school is selling sports packages with tickets to games for all of your favorite Atlanta teams. You have the option of choosing between 6 Falcons games, 4 Hawks games, and 9 Braves games. How many different packages could you create?
2. The math club is electing new officers. There are 3 candidates for president, 4 candidates for vice-president, 4 candidates for secretary, and 2 candidates for treasurer. How many different combinations of officers are possible?
3. A piggybank contains 2 quarters, 3 dimes, 4 nickels, and 5 pennies. One coin is removed at random.
 - a) What is the probability that the coin is a dime?
 - b) What is the probability that the coin is a dime or a nickel?
 - c) What is the probability that you choose a dime and then a penny? *(no replacement)*
 - d) What is the probability that the coin is not a dime?
 - e) Are the two events, selection of a dime and selection of a nickel, mutually exclusive? Explain.
4. Each of the letters of the word "GEOMETRY" is on a separate card. The cards have been mixed and placed in a box. If you select one card at random, what is the probability that its letter will be "E"?
5. A card is randomly selected from a standard deck of 52 cards. Find the indicated probability.
Hint: There are 4 jacks, 4 queens, 4 kings, 4 aces, 13 diamonds, 13 spades, 13 clubs, 13 hearts, 36 numbered cards, 26 red cards, and 26 black cards.
 - a) $P(\text{Jack})$
 - b) $P(\text{Ace or a Diamond})$
 - c) $P(\text{Red and King})$
 - d) $P(\text{Black card or Numbered card})$

6. Two cards are randomly selected from a standard deck of 52 cards (WITH REPLACEMENT). Find the indicated probability. ****Hint:** There are 4 jacks, 4 queens, 4 kings, 4 aces, 13 diamonds, 13 spades, 13 clubs, 13 hearts, 36 numbered cards, 26 red cards, and 26 black cards.**

a) $P(\text{Jack and Heart})$

b) $P(\text{Diamond and Diamond})$

c) $P(\text{Red and King})$

d) $P(\text{Black card and Numbered card})$

7. Two cards are randomly selected from a standard deck of 52 cards (**WITHOUT** REPLACEMENT). Find the indicated probability. ****Hint:** There are 4 jacks, 4 queens, 4 kings, 4 aces, 13 diamonds, 13 spades, 13 clubs, 13 hearts, 36 numbered cards, 26 red cards, and 26 black cards.**

a) $P(\text{Jack of Hearts and Heart})$

b) $P(\text{Ace and Ace})$

d) $P(\text{Black Card and Red King})$

d) $P(\text{Black Jack and Numbered card})$

- 8) The probability that a student with blue eyes is 35%. The probability that a student is over 6 feet tall and have blue eyes is 24%. What is the probability that a student is over 6 feet tall?

For #9 - 13, refer to the following table.

	Male	Female	Subtotal
Blue Eyes	10	30	
Green Eyes	20	60	
Subtotal			

9) $P(\text{Female}) =$

10. $P(\text{Blue Eyes}) =$

11. $P(\text{Blue Eyes} | \text{Female}) =$

12. $P(\text{Female} | \text{Blue Eyes}) =$

13. Are the events Female and Blue eyes independent? Explain.

key

1. Your school is selling sports packages with tickets to games for all of your favorite Atlanta teams. You have the option of choosing between 6 Falcons games, 4 Hawks games, and 9 Braves games. How many different packages could you create?

$$6 \cdot 4 \cdot 9 = 216$$

2. The math club is electing new officers. There are 3 candidates for president, 4 candidates for vice-president, 4 candidates for secretary, and 2 candidates for treasurer. How many different combinations of officers are possible?

$$3 \cdot 4 \cdot 4 \cdot 2 = 96$$

3. A piggybank contains 2 quarters, 3 dimes, 4 nickels, and 5 pennies. One coin is removed at random.

$$\text{total: } 14$$

- a) What is the probability that the coin is a dime?

$$\frac{3}{14}$$

- b) What is the probability that the coin is a dime or a nickel?

$$\frac{3}{14} + \frac{4}{14} = \frac{7}{14} = \boxed{\frac{1}{2}}$$

- c) What is the probability that you choose a dime and then a penny? (no replacement)

$$\frac{3}{14} \cdot \frac{5}{13} = \boxed{\frac{15}{182}}$$

- d) What is the probability that the coin is not a dime?

$$\boxed{\frac{11}{14}}$$

- e) Are the two events, selection of a dime and selection of a nickel, mutually exclusive? Explain.

yes mutually exclusive, b/c no coin can be both dime and nickel.

4. Each of the letters of the word "GEOMETRY" is on a separate card. The cards have been mixed and placed in a box. If you select one card at random, what is the probability that its letter will be "E"?

$$\frac{2}{8} = \boxed{\frac{1}{4}}$$

5. A card is randomly selected from a standard deck of 52 cards. Find the indicated probability.

****Hint:** There are 4 jacks, 4 queens, 4 kings, 4 aces, 13 diamonds, 13 spades, 13 clubs, 13 hearts, 36 numbered cards, 26 red cards, and 26 black cards.**

a) P(Jack) $\frac{4}{52} = \frac{1}{13}$

- b) P(Ace or a Diamond)

$$\frac{4}{52} + \frac{13}{52} - \frac{1}{52} = \frac{16}{52} = \boxed{\frac{4}{13}}$$

- c) P(Red and King)

$$\frac{2}{52} = \boxed{\frac{1}{26}}$$

- d) P(Black card or Numbered card)

$$\frac{26}{52} + \frac{36}{52} - \frac{18}{52} = \boxed{\frac{11}{13}}$$

52 * 52

6. Two cards are randomly selected from a standard deck of 52 cards (WITH REPLACEMENT). Find the indicated probability. **Hint: There are 4 jacks, 4 queens, 4 kings, 4 aces, 13 diamonds, 13 spades, 13 clubs, 13 hearts, 36 numbered cards, 26 red cards, and 26 black cards.**

a) P(Jack and Heart)

$$\frac{4}{52} \cdot \frac{13}{52} = \frac{1}{52}$$

b) P(Diamond and Diamond)

$$\frac{13}{52} \cdot \frac{13}{52} = \frac{1}{16}$$

c) P(Red and King)

$$\frac{26}{52} \cdot \frac{4}{52} = \frac{1}{26}$$

d) P(Black card and Numbered card)

$$\frac{26}{52} \cdot \frac{36}{52} = \frac{9}{26}$$

7. Two cards are randomly selected from a standard deck of 52 cards (WITHOUT REPLACEMENT). Find the indicated probability. **Hint: There are 4 jacks, 4 queens, 4 kings, 4 aces, 13 diamonds, 13 spades, 13 clubs, 13 hearts, 36 numbered cards, 26 red cards, and 26 black cards.**

a) P(Jack of Hearts and Heart)

$$\frac{1}{52} \cdot \frac{12}{51} = \frac{12}{2652} = \frac{1}{221}$$

b) P(Ace and Ace and Ace)

$$\frac{4}{52} \cdot \frac{3}{51} \cdot \frac{2}{50} = 0.00018 \quad \frac{24}{132600}$$

d) P(Black Card and Red King)

$$\frac{26}{52} \cdot \frac{2}{51} = \frac{1}{51}$$

d) P(Black Jack and Numbered card)

$$0.35 \quad \frac{2}{52} \cdot \frac{36}{51} = \frac{6}{221}$$

- 8) The probability that a student with blue eyes is 35%. The probability that a student is over 6 feet tall and have blue eyes is 24%. What is the probability that a student is over 6 feet tall?

0.24

$$P(6ft \text{ and } blue) = P(6ft) \cdot P(blue)$$

$$0.24 = P(6) \cdot 0.35$$

$$\frac{0.24}{0.35} = \frac{P(6) \cdot 0.35}{0.35}$$

$$\frac{0.24}{0.35} = P(6)$$

For #9 - 13, refer to the following table.

	Male	Female	Subtotal
Blue Eyes	10	30	40
Green Eyes	20	60	80
Subtotal	30	90	120

9) P(Female) =

$$\frac{90}{120} = \frac{3}{4}$$

$$P(6) = 0.686$$

10. P(Blue Eyes) =

$$\frac{40}{120} = \frac{1}{3}$$

11. P(Blue Eyes | Female) = $\frac{30}{90} = \frac{1}{3}$

denominator

12. P(Female | Blue Eyes) = $\frac{30}{40} = \frac{3}{4}$

13. Are the events Female and Blue eyes independent? Explain.

No

$$P(B|F) \neq P(F|B)$$